

B Mixing and Lifetimes With Exclusive and Inclusive Techniques



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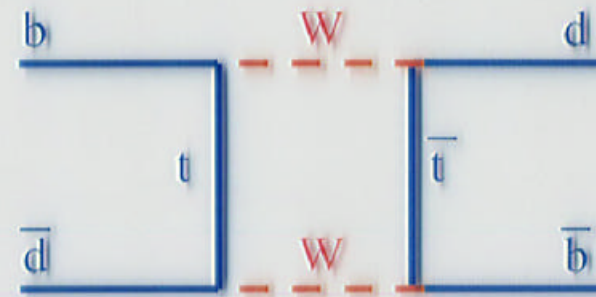


, Ise-Shima, Japan, Feb. 22nd 2001

Motivations

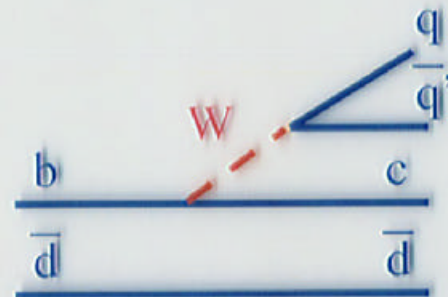
- **Mixing:**

- Constraint on the ρ - η plane
- Precision measurement at B-factories
- Validation for CP violation measurement



- **Lifetimes:**

- Tests of theoretical models of HQ decays
- Validation for CP violation measurement

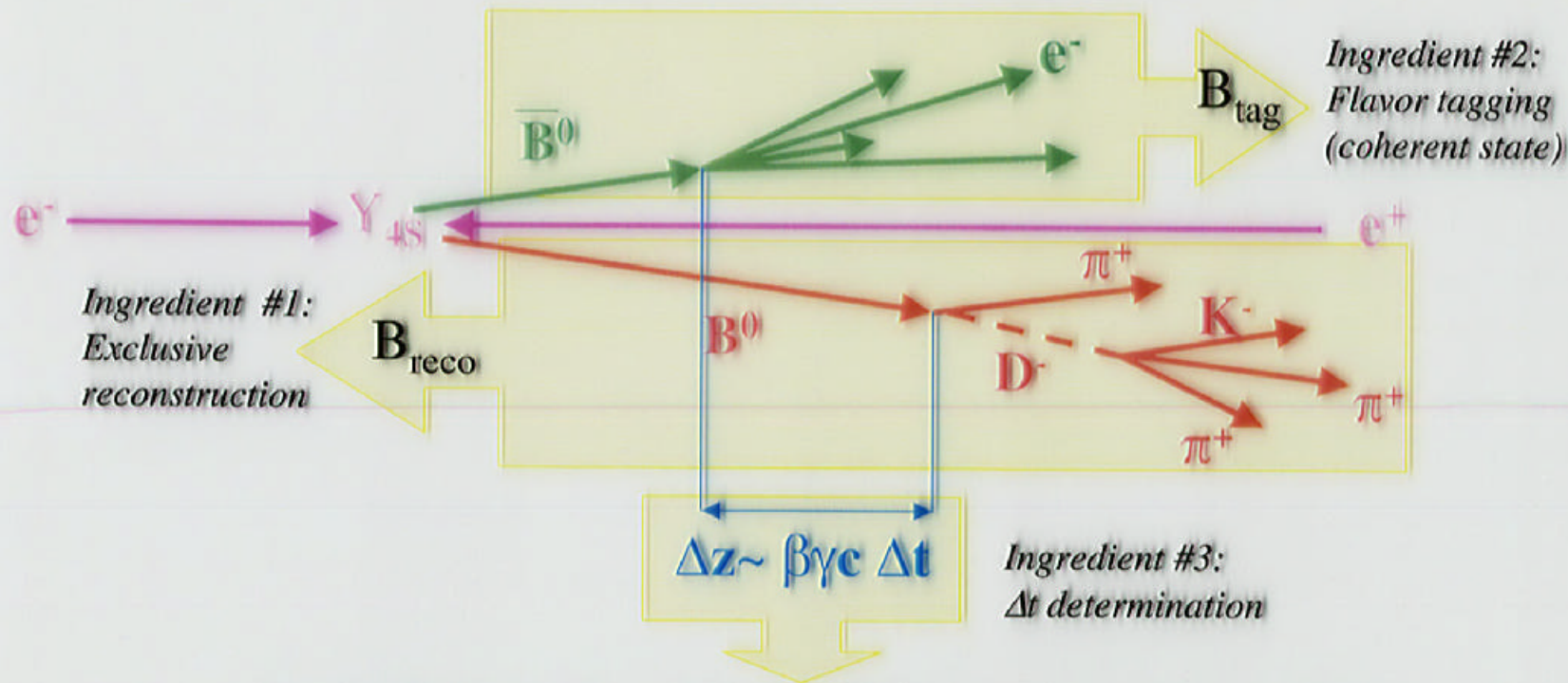


Experimental Techniques

1. Fully reconstructed hadronic B decays ($D^{(*)}\pi$, $D^{(*)}\rho$, $D^{(*)}a_1$, $J/\psi K^{*0}$)
 - Limited statistics (6k in 20fb-1)
 - Small systematics
 - Most similar to $\sin(2\beta)$
2. Partially reconstructed hadronic B decays
3. Fully or partially reconstructed $B \rightarrow D^* \ell \nu$
4. Dileptons
 - Large data sample (100k in 20fb-1, neutral and charged B in equal proportions)
 - Systematically limited (?)

Concentrate mostly on mixing from 1. and 4. in the following
WARNING: All results are PRELIMINARY !

Mixing With Fully Reconstructed Hadronic B Decays



$$h_{\pm}(\Delta t; \Gamma, \Delta m, \mathcal{D}) = 1/4 \Gamma e^{-\Gamma|\Delta t|} (1 \pm \mathcal{D} \cos(\Delta m \Delta t))$$

$$\text{Asymmetry} = \sim \mathcal{D} \cos(\Delta m \Delta t)$$

$$[\mathcal{D} = 1 - 2w, w = \text{mistag probability}]$$

(also add resolution function, backgrounds...)

Ingredient #1: B_{reco}

- Investigate the decays:

$$\bar{B}^0 \rightarrow D^{(*)+} \pi^-, D^{(*)+} \rho^-, D^{(*)+} a_1^-$$

$$\bar{B}^0 \rightarrow J/\psi K^{*0} \quad (K^{*0} \rightarrow K^+ \pi^-) \quad \text{see Andreas' talk}$$

- $D^{*+} \rightarrow D^0 \pi^+$
 - $D^0 \rightarrow K^- \pi^+, K^- \pi^+ \pi^+, K^- \pi^+ \pi^0, K_s^0 \pi^+ \pi^-$
- $D^+ \rightarrow K^- \pi^+ \pi^+, K_s^0 \pi^+$
- $\rho^- \rightarrow \pi^- \pi^0, K_s^0 \rightarrow \pi^+ \pi^-, \pi^0 \rightarrow \gamma\gamma, a_1^- \rightarrow \pi^- \pi^+ \pi^-$

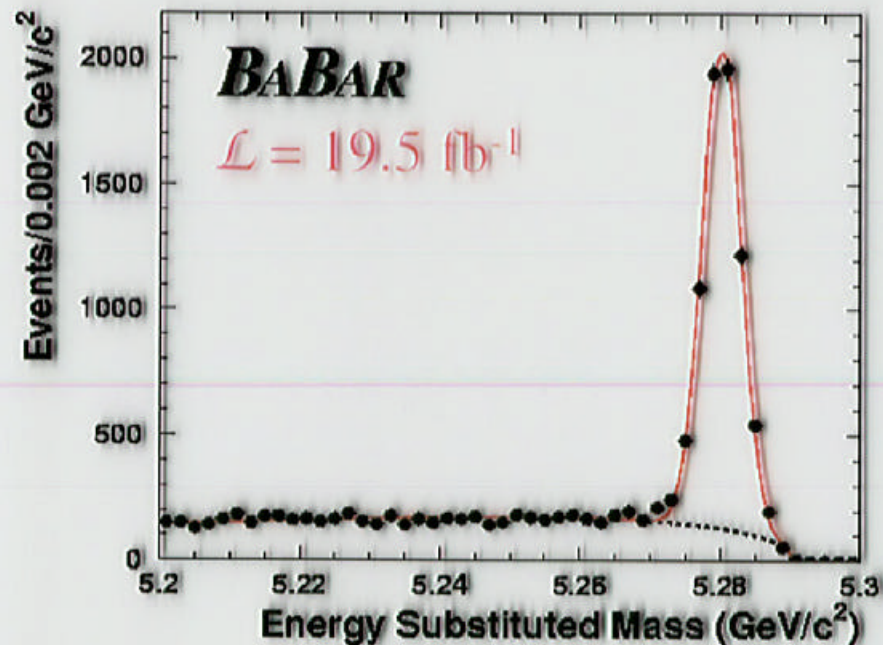
- Signal definition for B_{reco} :

- Define a window in the m_{ES} vs. ΔE plane:

$$m_{ES} = \sqrt{E_{beam}^{*2} - p_B^{*2}} \quad \Delta E = E_B^* - E_{beam}^*$$

$\sigma(m_{ES}) \sim 2.6$ MeV dominated by the beam energy spread
 $\sigma(\Delta E) \sim 20\text{-}30$ MeV (channel dependent)

Ingredient #1 (Cont.)



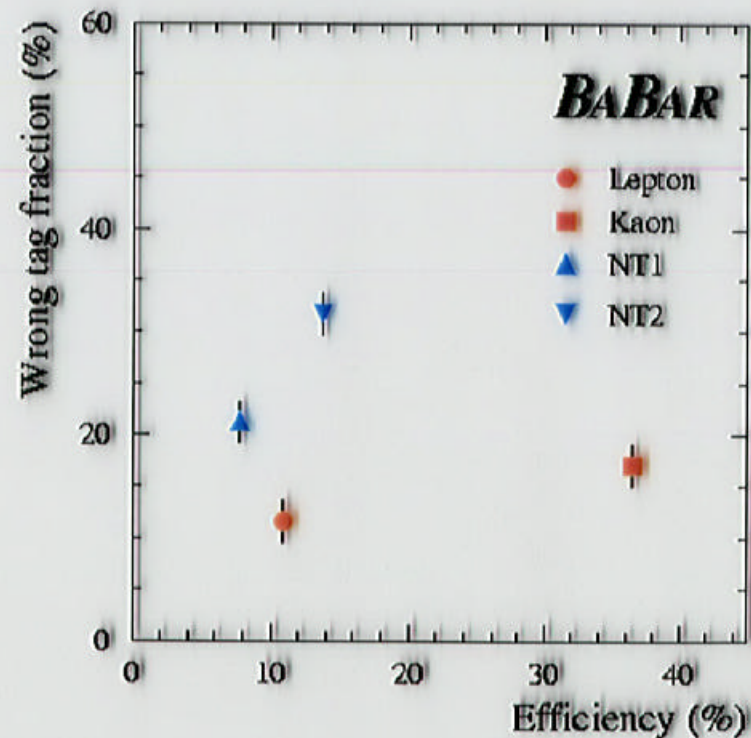
- $m_{ES} > 5.27 \text{ GeV}$
 - 6643 ± 96 signal events
 - 84% signal purity
- Combinatorial background:
 - Amount determined from m_{ES} fit
 - Time dependence: see later
- Peaking background
 - Due to pion swapping between the two B mesons
 - OK for neutral B
 - Add a background term in the fit for charged B (1-2%)

Ingredient #2: Tagging

- Analyze the remaining tracks of the event to determine the flavor of the B_{tag}
- 4 tagging categories
 - Primary lepton tag: $b \rightarrow c \ell^- \nu_\ell$ $p^*_\ell > 1.0$ GeV (e) or 1.1 GeV (μ)
 - Kaon tag: $b \rightarrow c X$; $c \rightarrow s X$; $s \rightarrow K^-$ (require $\Sigma Q_K \neq 0$)
 - NT1 and NT2: neural net
using other (correlated) info
(e.g. slow pions from D^* , ...)
- Prioritized algorithm
- Lepton and Kaon ID performance is crucial!

The effective tagging efficiency is

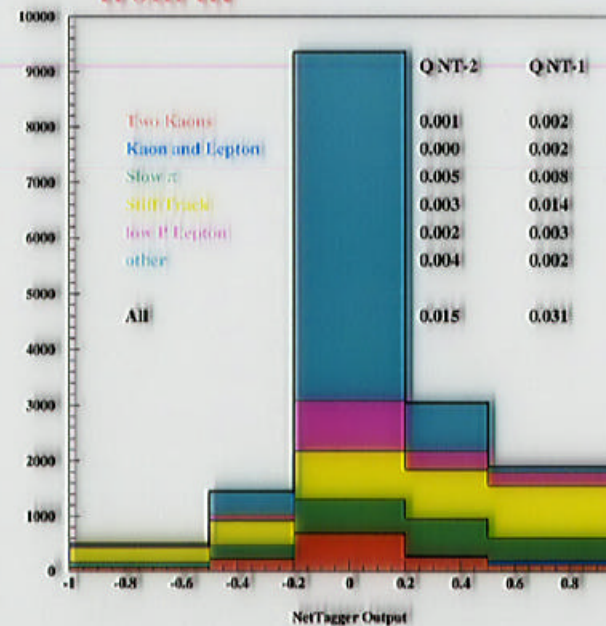
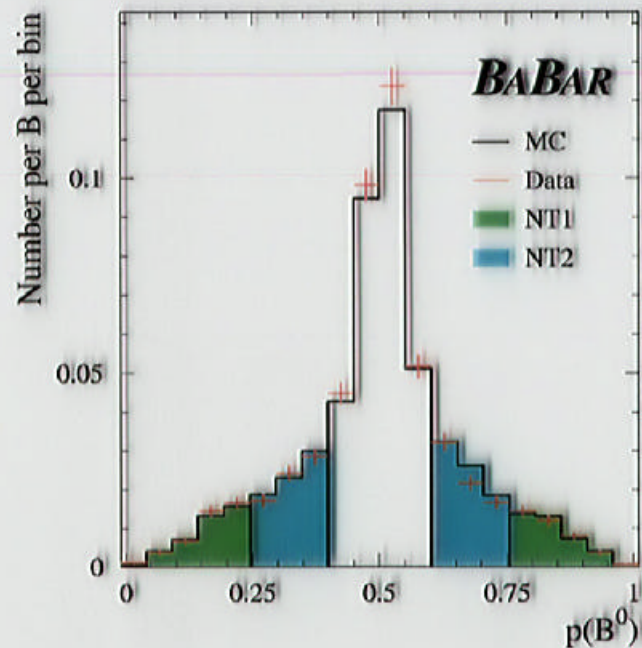
$$Q_i = e_i (1 - 2w_i)^2$$



Tagging performance

Category	Tagged Events	Efficiency(%)	Mistag (%)	Purity (%)
Lepton	754 ± 28	11.3 ± 0.4	8.5 ± 1.8	97.1 ± 0.6
Kaon	2317 ± 54	34.8 ± 0.6	16.7 ± 1.4	85.2 ± 0.8
NT1	556 ± 26	8.3 ± 0.3	19.5 ± 2.6	88.7 ± 1.5
NT2	910 ± 36	13.7 ± 0.4	32.6 ± 2.4	83.0 ± 1.3
Total	4538 ± 75	68.1 ± 0.9		86.7 ± 0.5

determined
from fit

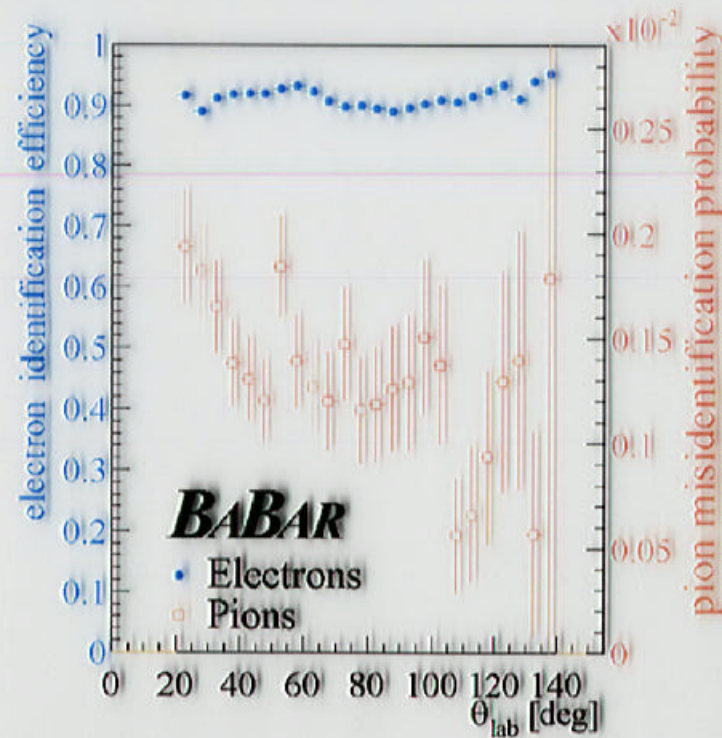
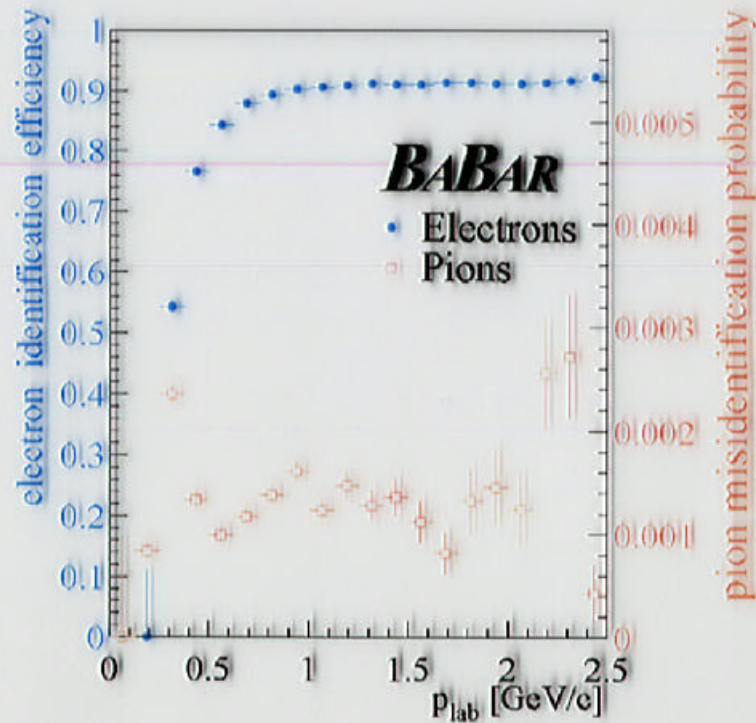


Particle ID in Babar

- Electron ID

$\epsilon=91\%$, π misid=0.13%

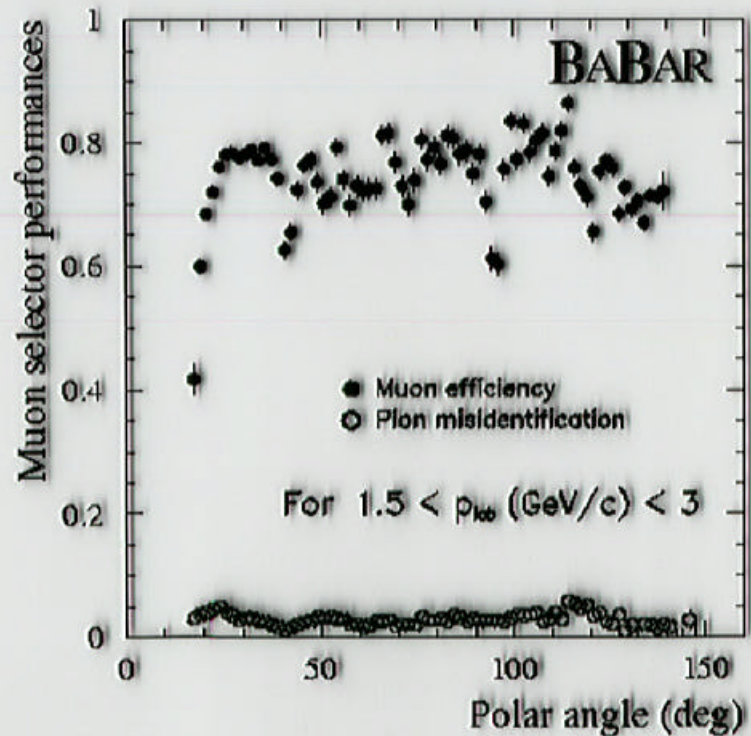
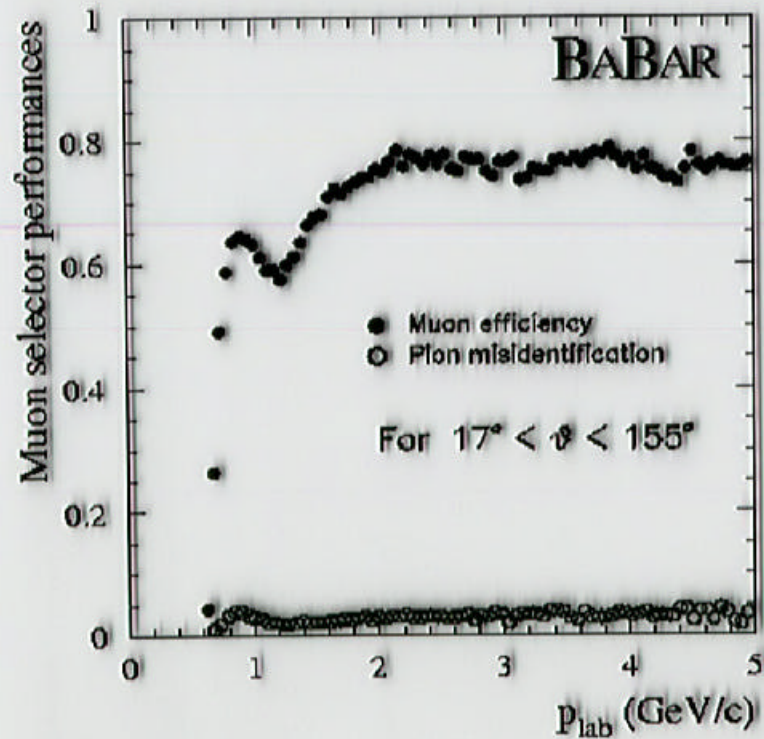
- Match track to EMC cluster
- $0.89 < E/p < 1.2$
- EM shower shape requirements
- dE/dx and DIRC \checkmark angle consistent with electron hypothesis



• Muon ID

$\epsilon=75\%$, π misid=2.5%

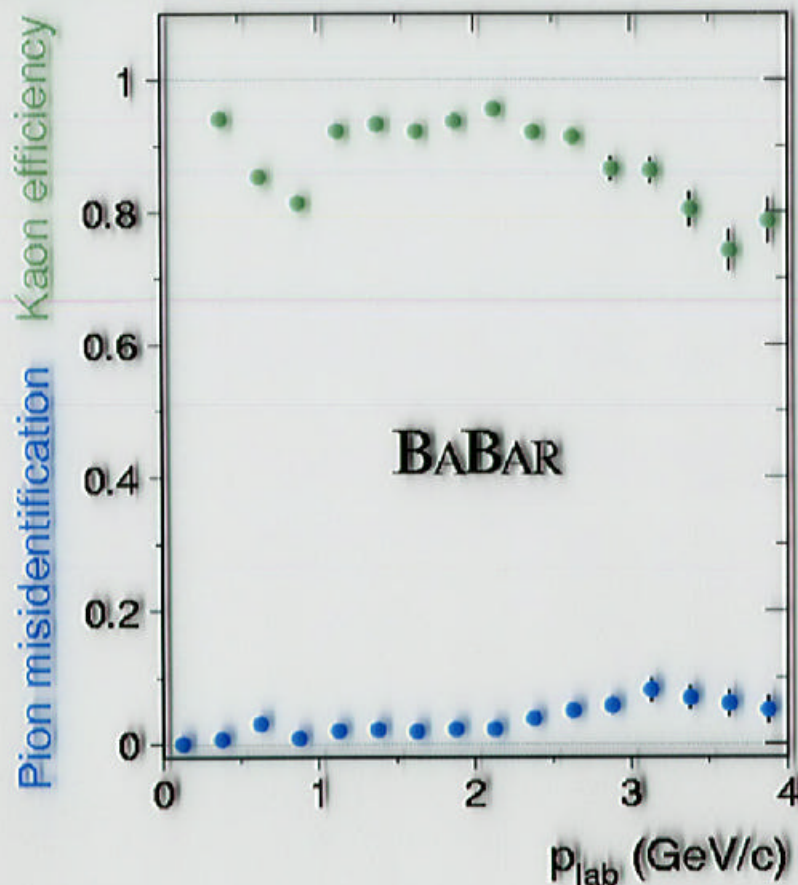
- # interaction lengths in IFR >2.2
- Difference in measured and expected int. Length <1
- Match between extrapolated track and IFR hits
- Requirements on average and spread of # of IFR hits per layer



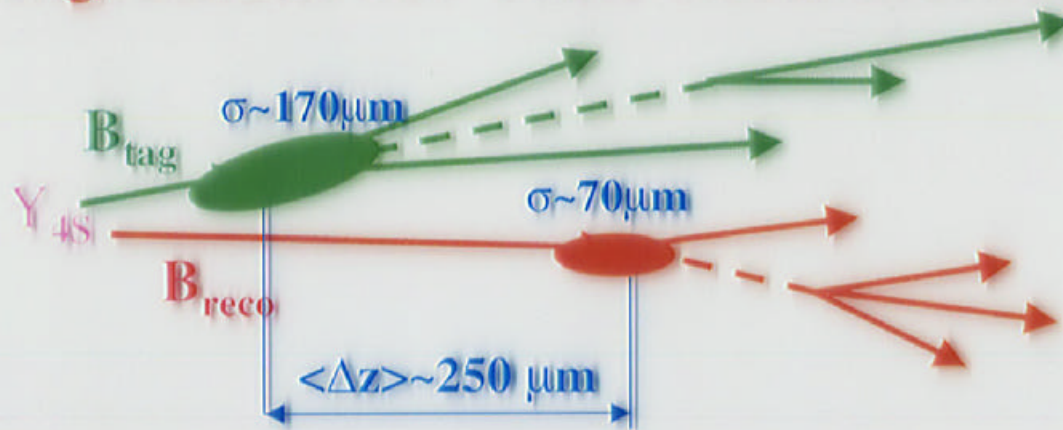
•Kaon ID

$\epsilon=85\%$, π misid=5%

- NN based on likelihood ratios in DCH and SVT (dE/dx), and in DIRC (compare single hits with expected pattern of Č light)
- $>3\sigma$ K/ π separation @ $0.25 < p < 3 \text{ GeV}$



Ingredient #3: Time Measurement



- B boosted along z axis: $\Delta t \sim \Delta z / (\beta\gamma c)$
- B_{reco} vertex explicitly reconstructed
- B_{tag} vertex inclusively reconstructed with all other tracks except B_{reco}
 - Kinematic constraint from B_{reco} momentum and decay vertex, beam spot and boost
 - Exclude tracks from charm ($\Delta\chi^2$ cut)
- Resolution function \mathcal{R} : 3 gaussians (core, tail, outlier)
 - Scale core/tail widths with event-by-event errors derived from vertex fits
 - Outlier (<1%): fixed width $\sigma \sim 8\text{ps}$
 - Allow different core biases depending on tagging categories
 - Fit parameters: scale factors, biases, relative core/tail/outlier amounts

Fitting Procedure

- Unbinned maximum likelihood fit to mixed-unmixed distributions

- Signal:

$$\mathcal{H}_{\pm,\text{sig}}(\Delta t; \Gamma, \Delta m, \mathcal{D}) = 1/4 \Gamma e^{-\Gamma|\Delta t|} (1 \pm \mathcal{D} \cos(\Delta m \Delta t)) \otimes \mathcal{R}(3\text{Gauss})$$

- Combinatorial background:

- Zero-lifetime component

$$\mathcal{B}_{\pm,1} = (1 \pm \mathcal{D}_1) \otimes \mathcal{R}_{\text{bek}}(2\text{Gauss})$$

- Non-oscillatory, non-zero lifetime component

$$\mathcal{B}_{\pm,2} = (1 \pm \mathcal{D}_2) \Gamma_2/2 e^{-\Gamma_2|\Delta t|} \otimes \mathcal{R}_{\text{bek}}(2\text{Gauss})$$

- Peaking background

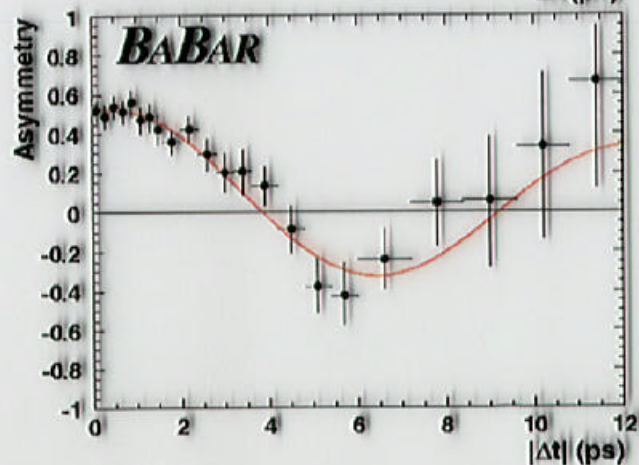
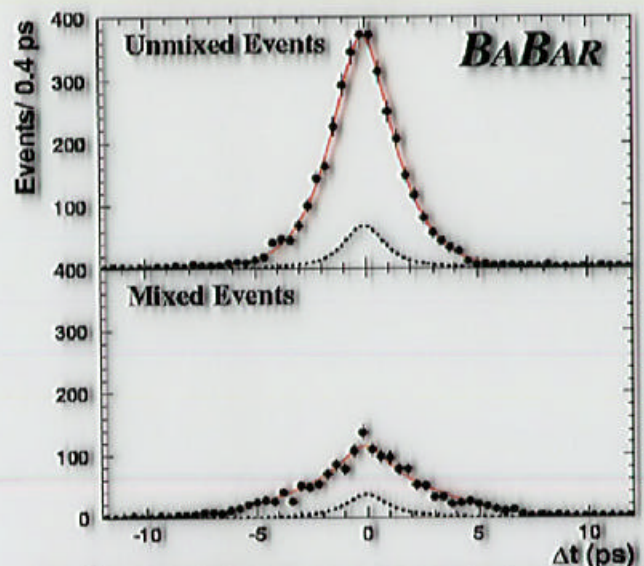
$$\mathcal{B}_{\pm,\text{charged}} = (1 \pm \mathcal{D}_+) \Gamma_+/2 e^{-\Gamma_+|\Delta t|} \otimes \mathcal{R}_{\text{sig}}(3\text{Gauss})$$

- $\mathcal{D}, \mathcal{D}_1, \mathcal{D}_2, \mathcal{D}_+$ split according to tagging categories
- 34 fit parameters

Fit Results

$\mathcal{L} = 19.5 \text{ fb}^{-1}$

$$\Delta m = (0.519 \pm 0.020 \pm 0.016) \text{ hps}^{-1}$$



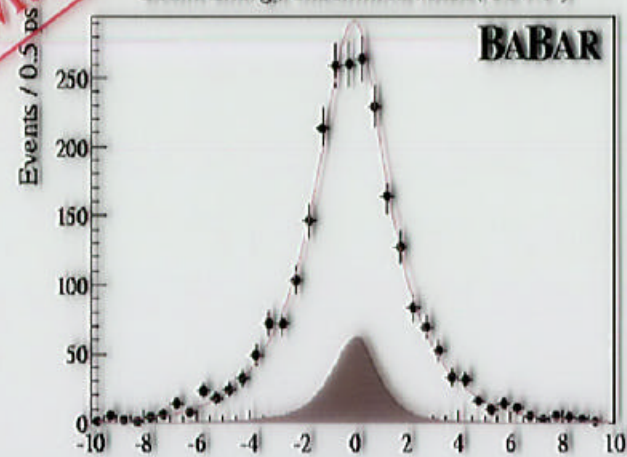
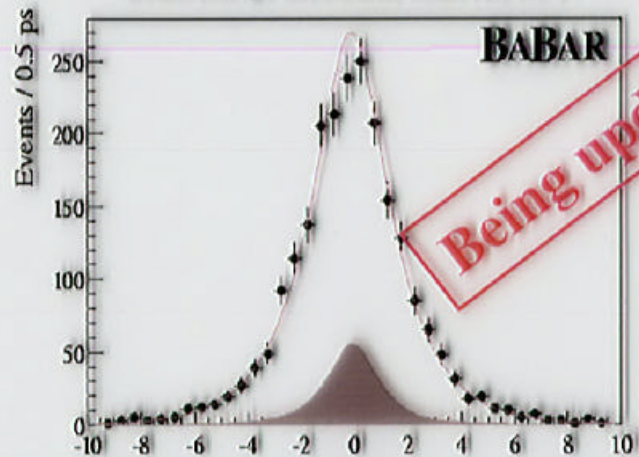
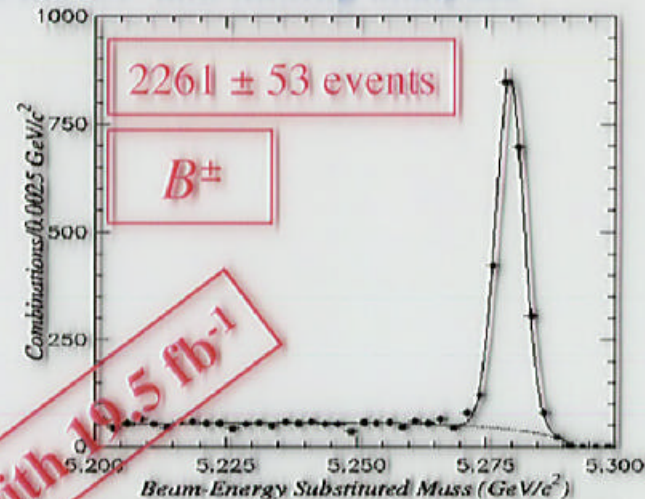
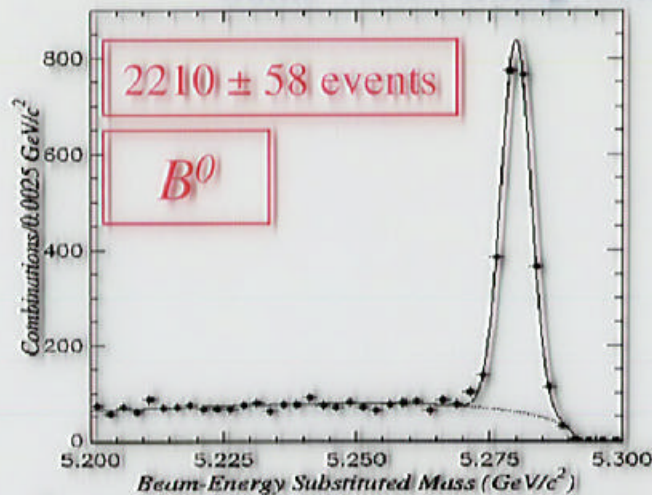
W_{lepton}	$= 0.085 \pm 0.018$
W_{kaon}	$= 0.167 \pm 0.014$
W_{NT1}	$= 0.195 \pm 0.026$
W_{NT2}	$= 0.326 \pm 0.024$

Source	$\Delta m [\text{hps}^{-1}]$
MC stats	0.004
MC correction	0.009
Δt outliers	0.002
Likelihood norm.	0.003
Background	0.005
B^0 lifetime	0.006
Z scale	< 0.005
Z boost	0.005
SVT alignment	0.004
Beamspot postn/size	0.001
Total	0.016

Lifetimes with fully reco hadronic decays

Same vertex fitting technique as the CP and mixing analyses

7.4 fb⁻¹ on peak

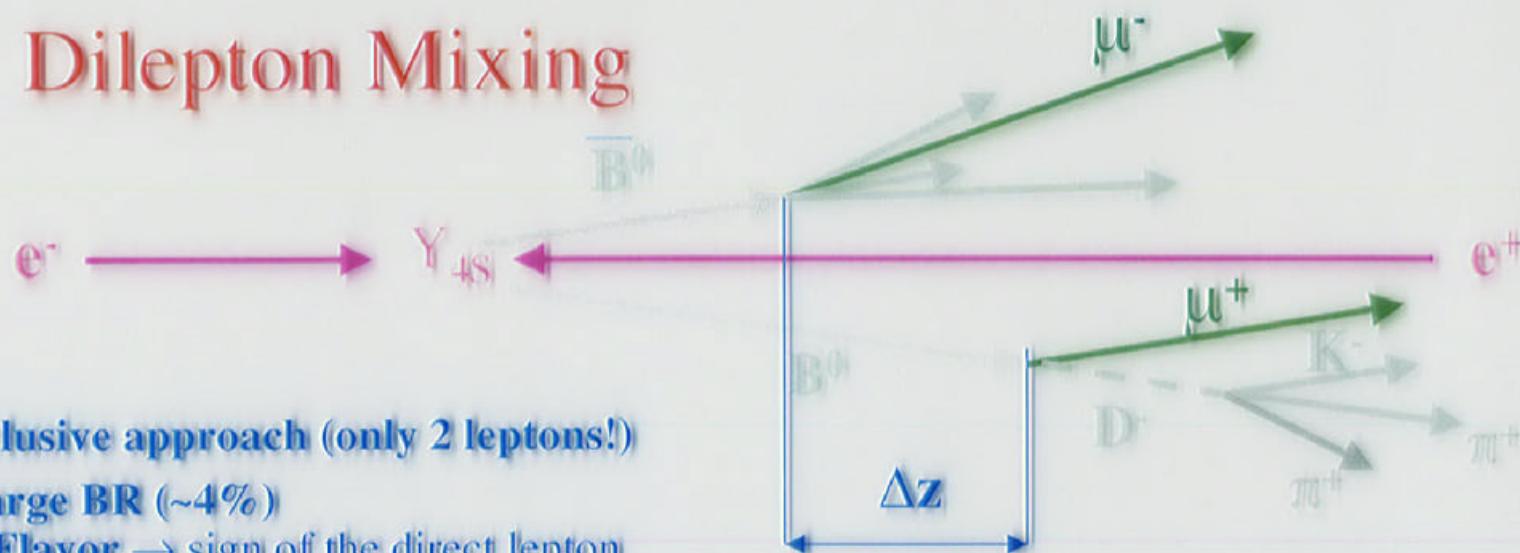


$$\tau_{B^0} = 1.506 \pm 0.052 \text{ (stat)} \pm 0.029 \text{ (syst)} \text{ ps} \quad \tau_{B^\pm} = 1.602 \pm 0.049 \text{ (stat)} \pm 0.035 \text{ (syst)} \text{ ps}$$

$$\tau_{B^\pm} / \tau_{B^0} = 1.065 \pm 0.044 \text{ (stat)} \pm 0.021 \text{ (syst)}$$

Being updated with 19.5 fb⁻¹

Dilepton Mixing



- **Inclusive approach (only 2 leptons!)**
- **Large BR (~4%)**
- **B Flavor** → sign of the direct lepton
- **B^0 and B^\pm admixture** → Fraction R fitted
- Δz → **points of closest approach of the leptons to the beam spot in transverse plane**

$$A(\Delta t) = \frac{N(l^+ l^-)(\Delta t) - N(l^\pm l^\pm)(\Delta t)}{N(l^+ l^-)(\Delta t) + N(l^\pm l^\pm)(\Delta t)}$$

2 additional parameters in the fit to take into account the fraction of mistagged events (cascade leptons).

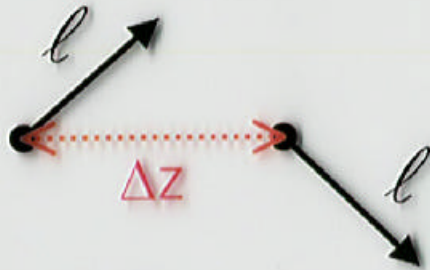
Fit of Δm and the fraction R

$$A(\Delta t) = \frac{e^{-\Gamma^0 |\Delta t|} \cos(\Delta m_B \Delta t) + R \cdot e^{-\Gamma^\pm |\Delta t|}}{e^{-\Gamma^0 |\Delta t|} + R \cdot e^{-\Gamma^\pm |\Delta t|}}$$

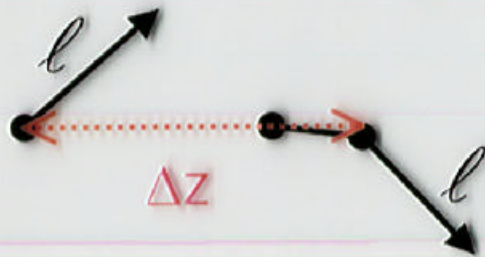
Dilepton Mixing: Event selection

- Continuum background rejection: event shape variables
- Rejection of J/ψ and conversions with invariant mass cut
- cuts on track quality (SVT z hits, polar angle, Δz error)
- NN to select signal events (lepton p^* and opening angle, total energy and missing momentum of the event)
- sample composition: 78% signal, 12% direct-cascade, 5% with one or more fake leptons, 5% continuum + other
- Eventually increase neutral B purity by inclusively reconstructing the $B \rightarrow D^* \ell \nu$ decay with a soft pion from D^*

Signal and (main) backgrounds



- Direct leptons (78%)
 - sensitive to mixing (!)
 - B-lifetime component

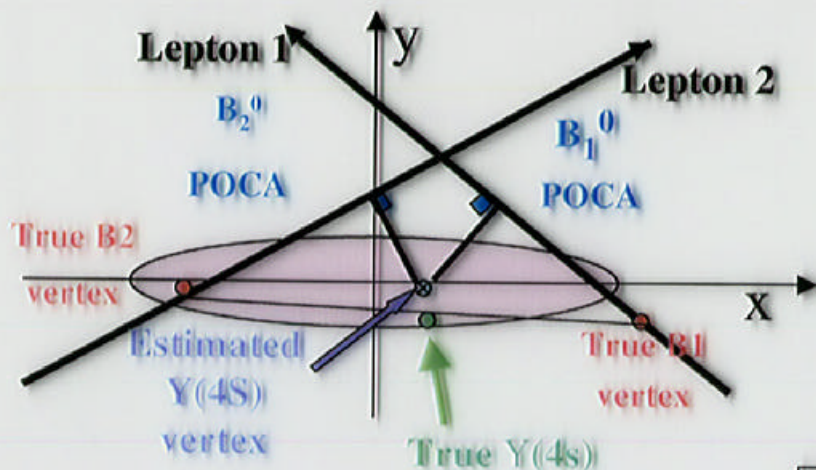


- Opposite-B cascade (OBC) leptons (~7%)
 - sensitive to mixing, but
 - source of mistag (~100%)
 - extra-lifetime due to charm decay (B-lifetime + effective lifetime from charm)



- Same-B cascade (SBC) leptons (~5%)
 - not sensitive to mixing
 - source of opposite-sign leptons only
 - effective lifetime from charm
- Misidentified leptons (~5%):
 - same topologies (and resolution function) as above
 - extra mistag to be taken into account
- Continuum (~5%): fit off-resonance data

Dilepton Mixing: Δt measurement



Δz = z difference of the point of closest approach (POCA) of the tracks to a Y(4S) vertex, estimated with the 2 leptons and a beam spot constraint

Agreement within 10%

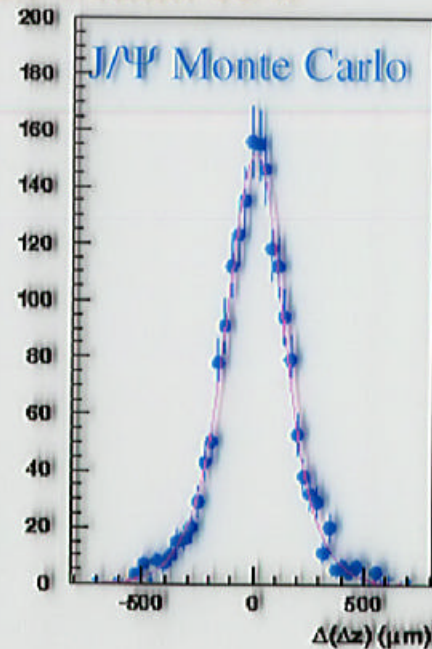
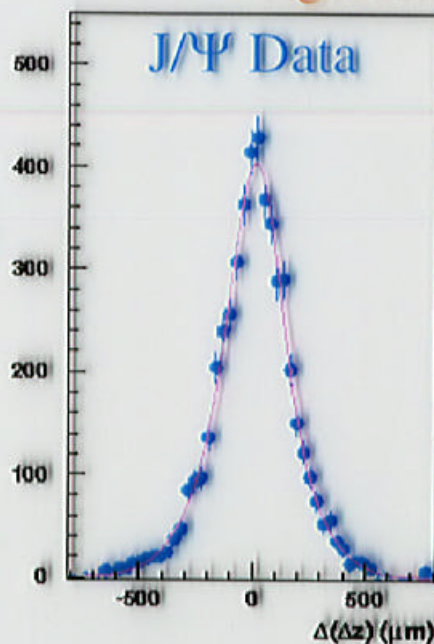
- Δz resolution function determined with MC and cross-checked with J/ Ψ .

Narrow Gaussian : 87 μ m (76%)

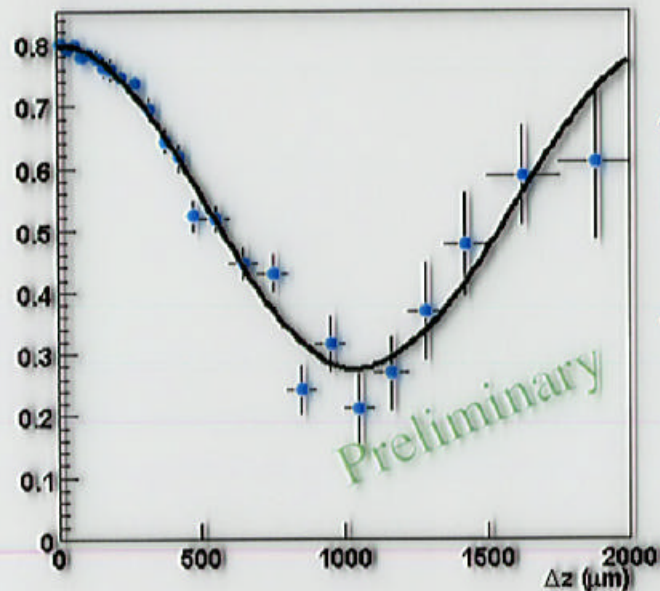
Wide Gaussian : 195 μ m (24%)

- Boost approximation:

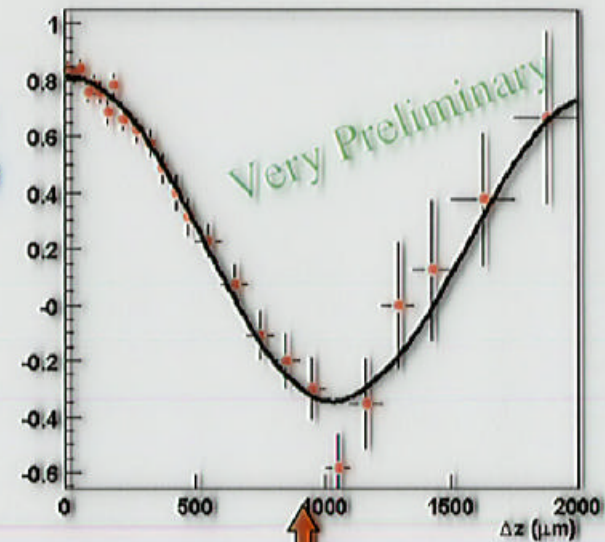
$$\Delta t = \Delta z / (c \langle \beta \gamma \rangle)$$



Dilepton Mixing: Results



7.7 fb⁻¹ on-resonance
1.1 fb⁻¹ off-resonance
~35000 events



$$\Delta m_d = (0.507 \pm 0.015(\text{stat}) \pm 0.022(\text{syst})) \hbar \text{ ps}^{-1}$$

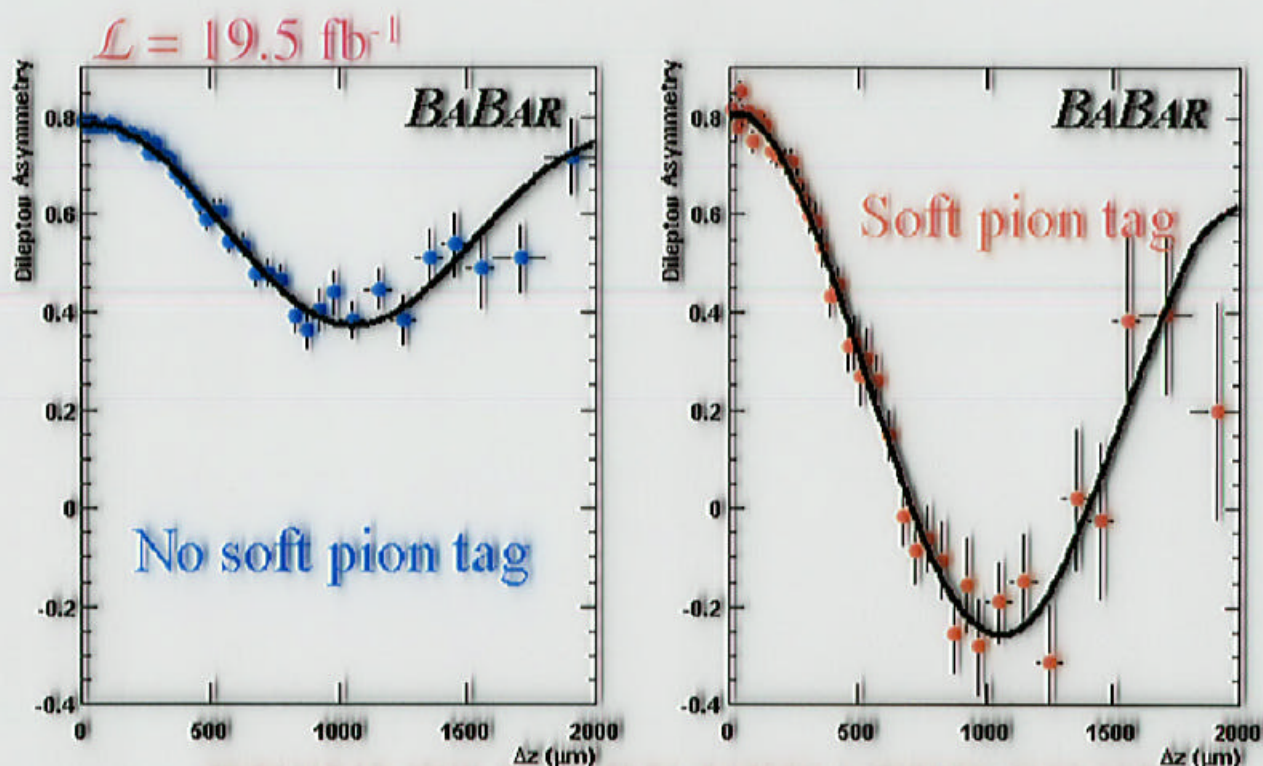
Dilepton sub-sample enriched in
 B^0 with partial reconstruction
of $B^0 \rightarrow D^* l \nu$ (soft pion tag)

Systematic uncertainties dominated by

- lepton misID
- cascades parametrization
- Δz resolution function
- B meson lifetimes

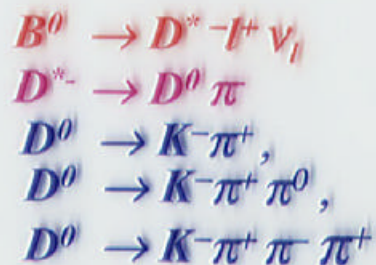
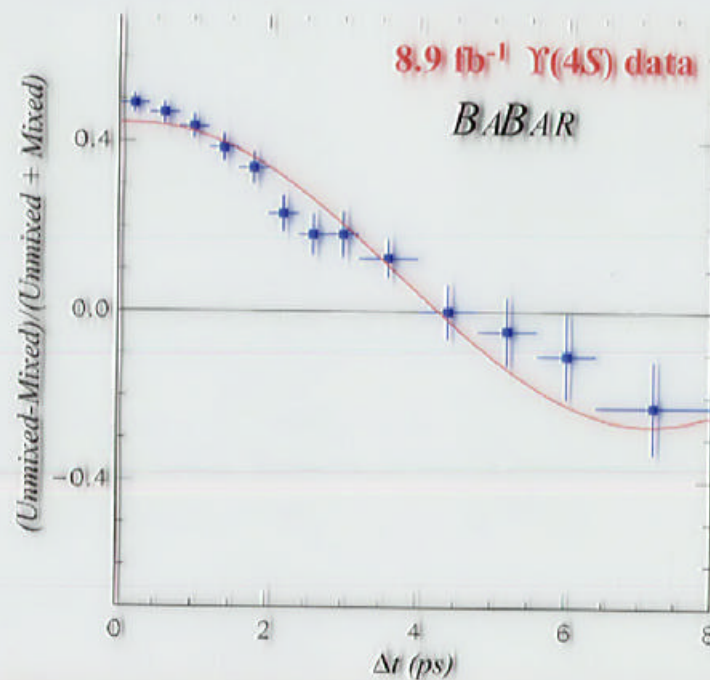
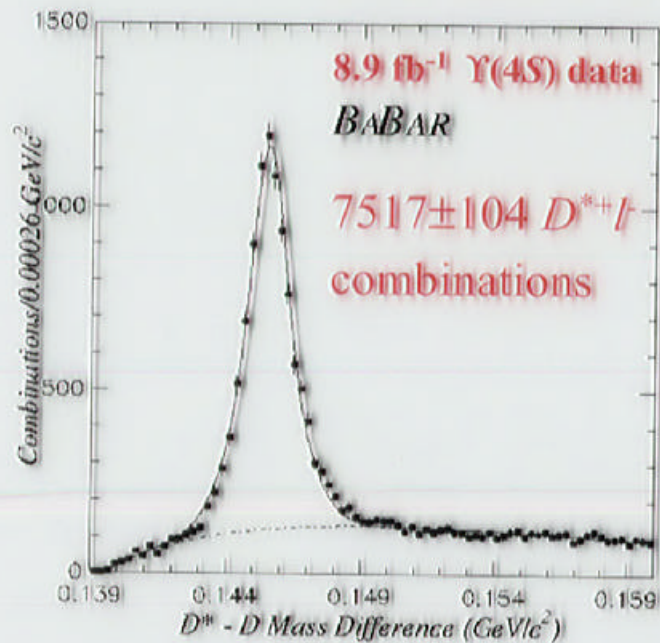
Dilepton Mixing Prospects With Run1 Data

- From 7 to 20 fb⁻¹ (~100K events): *statistical error* 0.015 → 0.010 $\hbar ps^{-1}$
- Improve background description and fitting technique and strategy to reduce *systematic error*: 0.022 → <0.010 $\hbar ps^{-1}$



RESULTS TO BE UPDATED SOON !

Mixing with fully reco $B \rightarrow D^* \ell \nu$



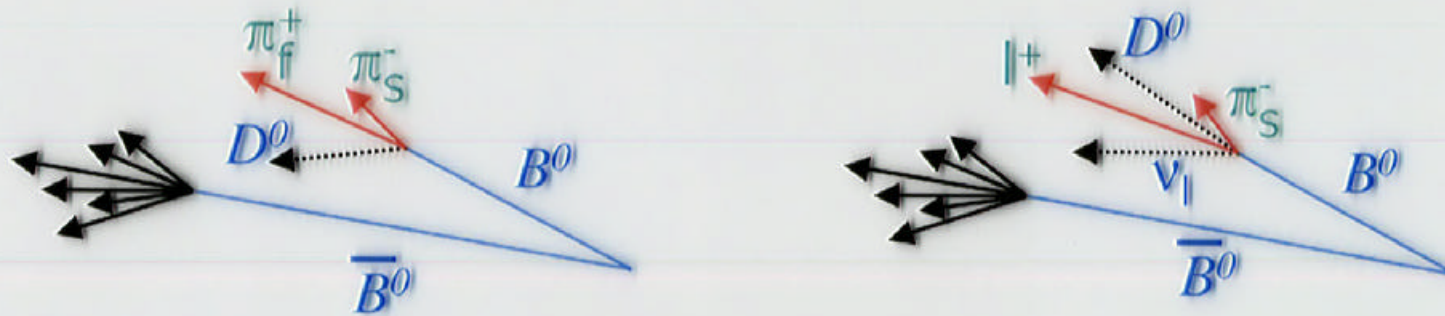
$$\Delta m_d = (0.508 \pm 0.020(\text{stat}) \pm 0.022(\text{syst})) \hbar \text{ ps}^{-1}$$

(Being updated with 19.5 fb⁻¹)

Lifetimes and mixing with partial reco methods

$$B^0 \rightarrow D^{*-} \pi_f^+$$

$$B^0 \rightarrow D^{*-} l^+ \nu_l$$



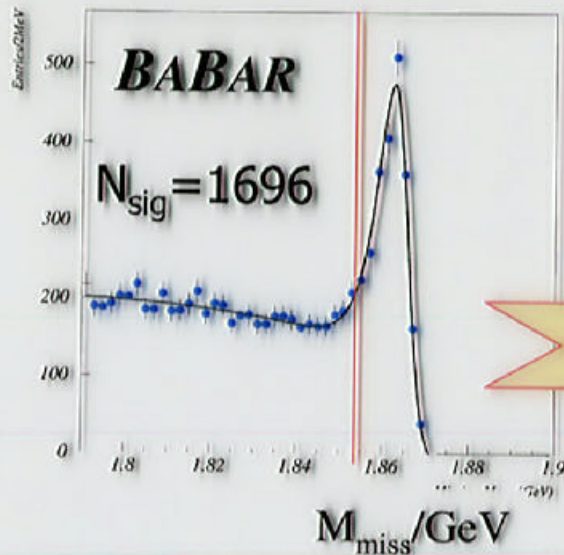
High statistics

- ❑ Reconstruct M_{miss} from π^+ and π^- only.
- ❑ Use beam constraints

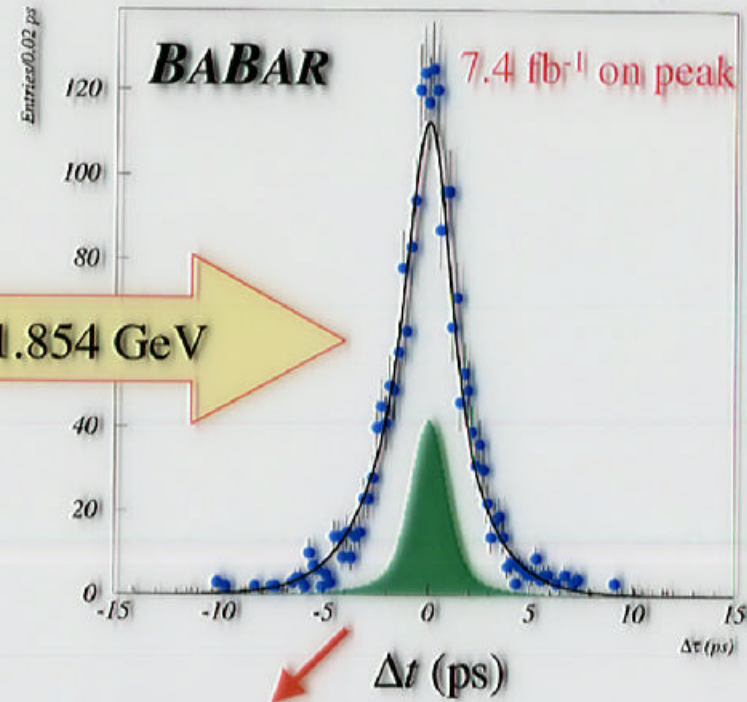
- π_S^- direction $\approx D^{*-}$ direction.
- Reconstruct m_{ν}^2 from l^+ and π^- only.

B^0 lifetime with $B^0 \rightarrow D^{*-} \pi^+$

Unbinned maximum likelihood fit.



$M_{\text{miss}} > 1.854$ GeV



27% background

Selection:

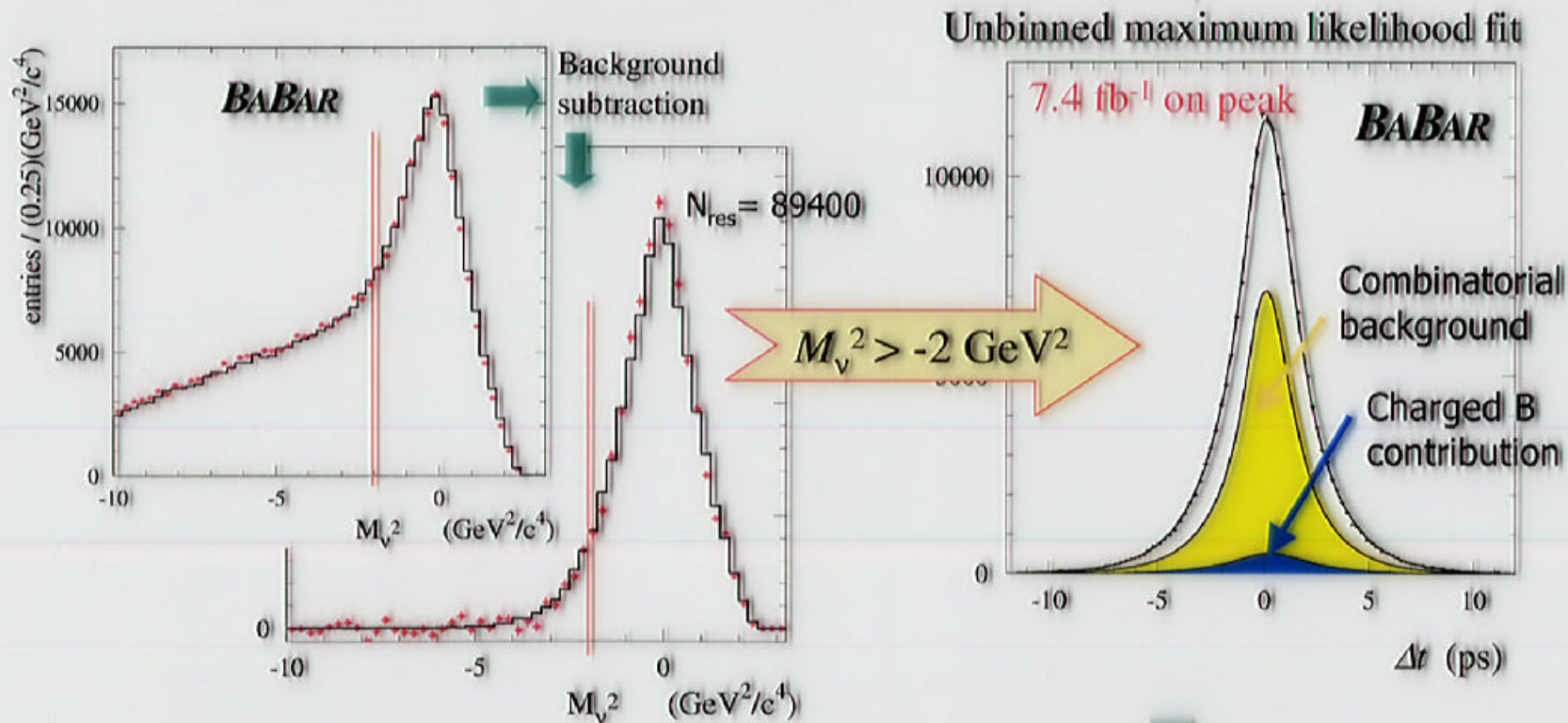
- Kinematics: $2.114 < p_{\pi^+} < 2.404$ GeV
 - Event shape $R_2 < 0.35$
 - π^+ isolation (0.4 rad)
 - Fisher discriminant
 - Helicity angle $|\cos \psi| > 0.4$
- ⇒ Efficiency = 16 %



$$\tau = 1.55 \pm 0.05 \text{ (stat)} \\ \pm 0.07 \text{ (syst) ps}$$

(Being updated with 19.5 fb⁻¹)

B^0 lifetime with $B^0 \rightarrow D^{*-} l^+ \nu_l$

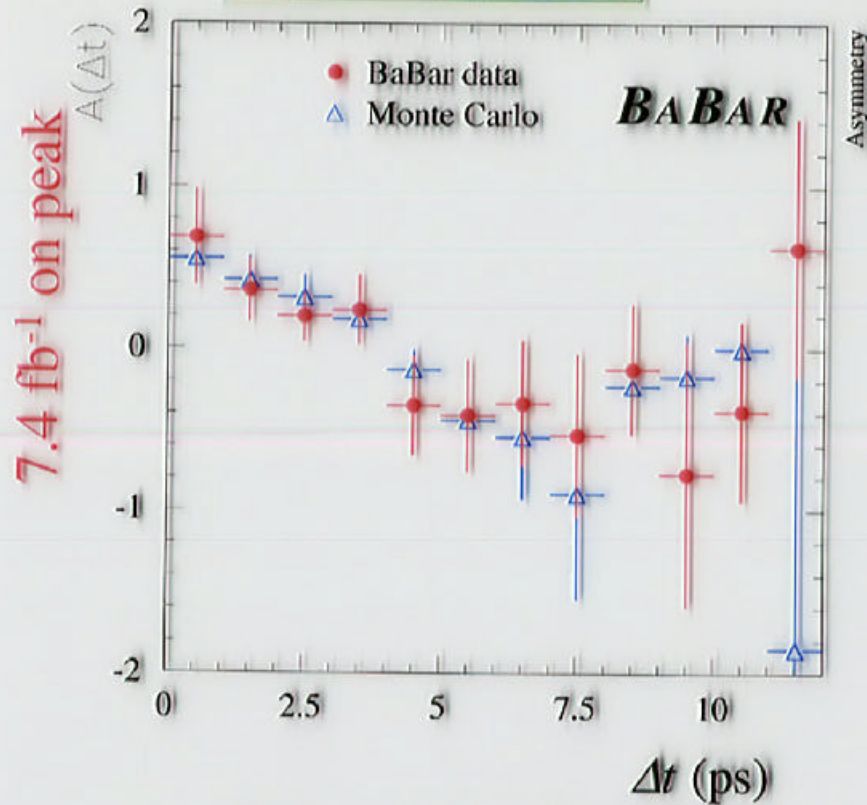


- Background determined by same sign events ($l^+ \pi_s^+$, $l^+ \pi_s^-$)
- Charged B contamination: 5 %
- Combinatorial background: 40.7 %

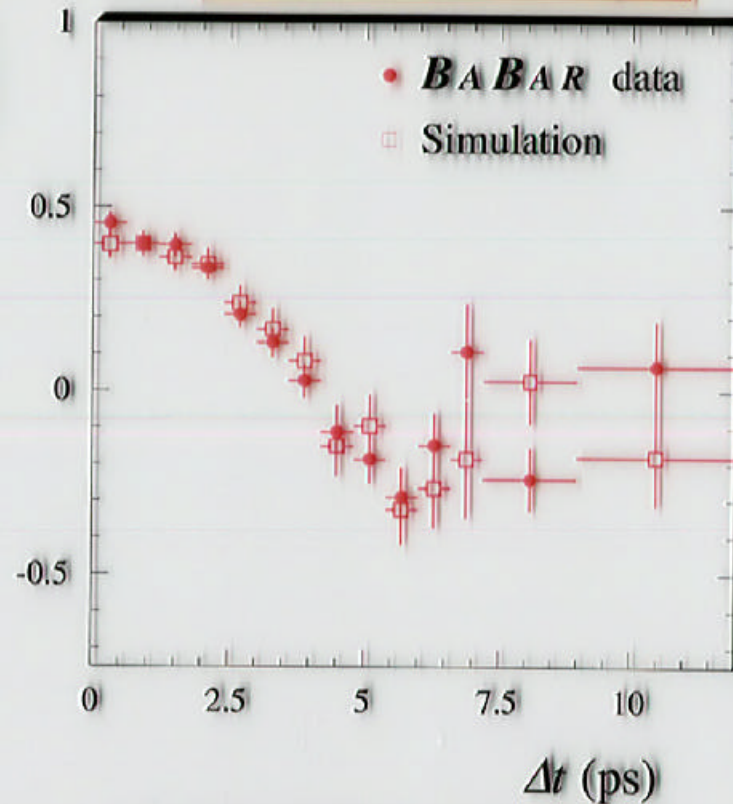
$$\tau = 1.63 \pm 0.02 \text{ (stat)} \\ \pm 0.09 \text{ (syst) ps}$$

(Being updated with 19.5 fb⁻¹)

B^0 mixing with partial reco methods



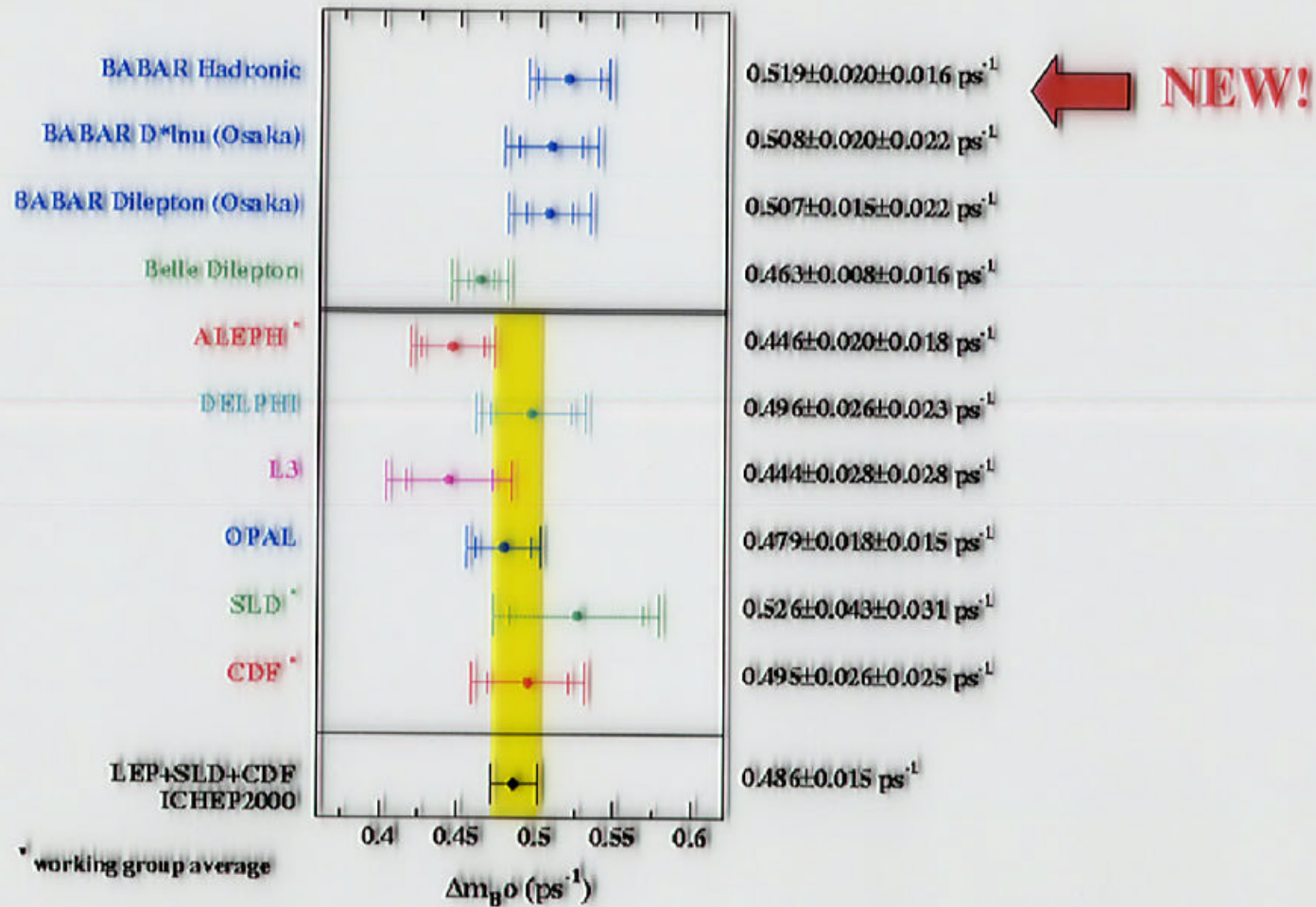
• Background subtraction applied



• Combinatorial background subtracted

➔ Mixing signal is seen

Mixing measurements



Conclusion

- Precise measurements of lifetimes and mixing with 4 different techniques!
 - Any single measurement as accurate as the pre-B-factory-era world average
- New result on hadronic mixing
$$\Delta m = (0.519 \pm 0.020 \pm 0.016) \hbar ps^{-1}$$
 - Validates detector performance for $\sin(2\beta)$ measurement
- Other results to be updated/published in a short time