

BCP4  
Ise, 19-23 Feb. 01

SUSY CONTRIBUTIONS TO  
LOW ENERGY OBSERVABLES

OF

THE PRE-LHC SUSY  
CHALLENGE

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SISSA & INFN TRIESTE

MECHANISMS  $\begin{cases} \text{FLAVOR STRUCTURE } (m_f, CKM, m_f, \dots) \\ \text{SUSY BREAKING} \end{cases}$

↓  
implications if they are or are not related  
for FCNC,  $CP_f$ ,  $a_\mu$  in the pre-LHC epoch

# LOW ENERGY SUSY

WHY

- GAUGE HIERARCHY PROBLEM
- UNIFICATION OF STRONG + ELW. INTER.
- ONLY COMPLETE, PHENOMENOLOGICALLY VIABLE THEORY OF NEW PHYSICS AT  $O(\text{TeV})$

SIGNATURE

- MOST (but not necessarily all) SUSY PARTICLES HAVE A MASS  $\lesssim O(1 \text{ TeV})$ 
  - ⚡ doubling of known particles with the same  $SU(3)$ ,  $SU(2)$ ,  $U(1)$ , flavor, ... numbers

HOW TO

FIND IT

## DIRECT SEARCHES

production and observation of s-particles

limits:  $m_{\text{colored s-part}} > 200-250 \text{ GeV}$

$m_{\tilde{e}, \text{chargino}} > m_Z$

$m_{\text{lightest neutralino LSP}} > 40 \text{ GeV}$   
( $m_H \sim 115 \text{ GeV}?$  → favors SUSY)

INDIRECT SEARCHES FCNC, CP, g-2

# MINIMAL LOW ENERGY SUSY

↙ - minimal amount of superpart. needed to supersymmetrize the SM

- IMPOSING THE (ADDITIONAL) SYMM.  $R$  parity  
 ⇒ to eliminate  $B$  and  $L \neq$  dangerous terms

$$\mathcal{L} = \mathcal{L}_{N=1 \text{ SUSY SM}}$$



$$\dots h_{U_{ij}} \bar{Q}_i H_U U_j + h_{D_{ij}} \bar{Q}_i H_D D_j + h_{L_{ij}} \bar{L}_i H_D E_j + \mu H_U H_D$$

$$+ \mathcal{L}_{\text{soft SUSY breaking}}$$



trilinear and bilinear scalar terms + gaugino masses



$$m_{ij}^2 \varphi_i \varphi_j^*$$

$$\mu B H_U H_D$$

$$A_{U_{ij}} \bar{Q}_i H_U \tilde{U}_j$$

$$A_{D_{ij}} \bar{Q}_i H_D D_j$$

$$A_{L_{ij}} \bar{L}_i H_D \tilde{E}_j$$

$$M_k \lambda_k \lambda_k$$

↳  $SU(3), SU(2), U(1)$



124 PARAM.

# CMSSM

or

# mSUGRA

↳ Constrained

minimal SuperGravity

or how to reduce the param. from **124** → **5**

## MSSM

+

### FLAVOR UNIVERSALITY

### (GRAND) UNIFICATION



$$m_{ij}^2 = \delta_{ij} m_0^2$$

Common scalar mass term

$$A_{ij} \rightarrow A_0$$

Common scalar trilinear coeff. multiplying the Yukawa coupl.



$$M_1 = M_2 = M_3 = M$$

Common gaugino mass

$m_{ij}^2, A_{ij}, M_i \Rightarrow$  "running" quantities: specify the energy scale where the above equalities hold

➔ **BOUNDARY CONDITIONS AT THE LARGE SCALE WHERE SUPERGRAVITY IS BROKEN**  $M_X$

at  $M_X$ :  $m_0^2, \mu, B_0, A_0, M$

# NEW $CP \neq$ in SUSY

unconstrained  
MSSM  $\Rightarrow \sim 40$  phases

mSUGRA  $\Rightarrow \mu, M, A, B$  4 phases  
but only 2 combinations  
are physical

Dugan, Grinstein,  
Hall;  
Dimopoulos, Thomas

- \* THE PRESENCE OF LOW ENERGY SUSY
- \* ENTAILS THE PRESENCE OF (AT LEAST TWO)
- \* NEW  $CP \neq$  PHASES IN ADDITION TO
- \* THE CKM PHASE

THE PRESENCE OF NEW SOURCES OF  $CP \neq$  IS  
NEEDED TO HAVE AN EFFICIENT BARYOGENESIS

(in SM no significant baryogenesis is possible;  
in CMSSM only a very limited area of the parameter space  
is available for baryogenesis  $\Rightarrow$  light  $\tilde{t}, \tilde{t}^+$ )

# CMSSM WITH $\phi_A, \phi_\mu \neq 0$

'83 Frère and Gavela : is it possible to put  $\delta_{CKM} = 0$   
and explain  $\epsilon$  only as a SUSY effect?

Dugan, Grinstein, Hall : **NO**  $\Rightarrow \phi_A, \phi_\mu$  too small because of  $d_n^e$

NEW DEVELOPMENTS ON THE THEME **LARGE SUSY CP  $\neq$**

**PHASES WHILE TAKING THE  $d_n^e$**



**CANCELLATIONS  
AMONG THE SUSY  
CONTRIBUTIONS TO  $d_n^e$**

Ibrahim, Nath;  
Brhlik, Good, Kane;  
Brhlik, Everett, Kane, Lykken;  
Accomando, Arnowitt, Dutta

need for non-universal  
gaugino masses  $\Rightarrow$  SUGRA GUT  
disfavored, D-branes within  
Type I strings favored

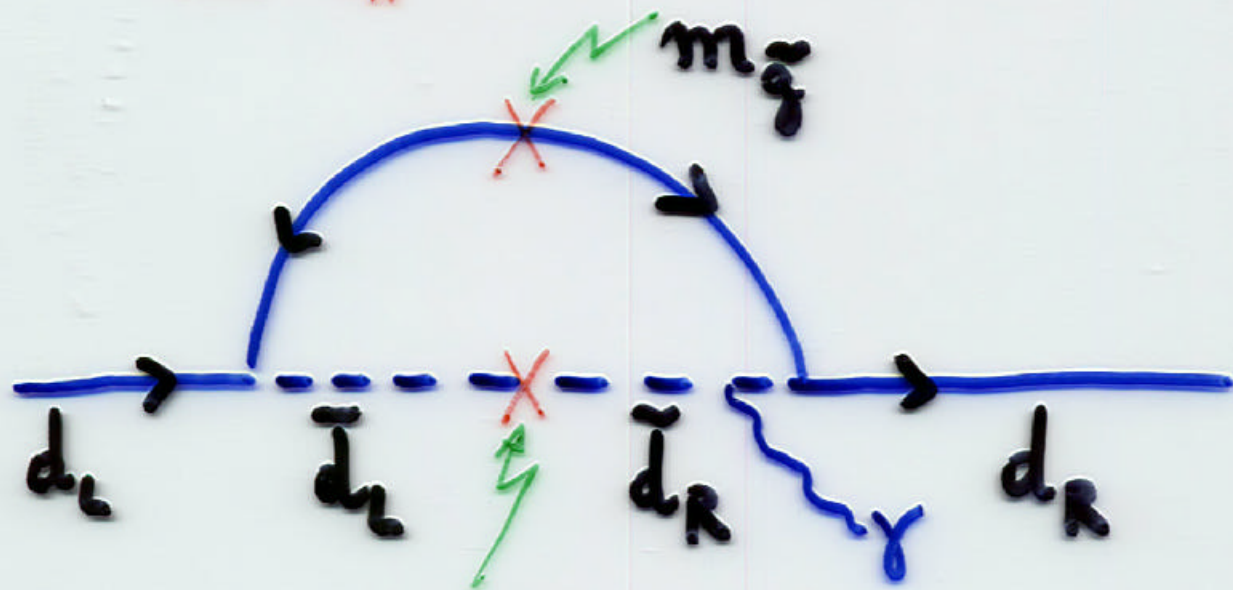
**LARGE MASSES  
OF  $\tilde{Q}$   
OF THE FIRST**

**TWO GENERATIONS**

Dimopoulos, Giudice;  
Tomarol, Tommasini;  
Dine, Kagan, Samuel;  
Dine, Kagan, Leigh;  
Carena et al.;  
J.E. Kaplan et al

**NON-UNIVERS.  
OF THE  
A-TERMS**

Abel, Frère;  
Khalil, A.M.  
Kobayashi;  
Khalil,  
Kobayashi,  
Vives

THE  $d_N$  SUSY PROBLEM

$$A m_d + m_d \mu \tan \beta$$

$$\tan \beta = \frac{v_u}{v_d}$$

$$d_d = \frac{m_d}{\tilde{m}^2} \frac{e v_d}{48 \pi} \left( |A m_g| \sin \phi_A + \tan \beta |\mu m_g| \sin \phi_B \right)$$

taking  $m_{\tilde{d}_L}^2 \sim m_{\tilde{d}_R}^2 \sim m_{\tilde{g}}^2 \sim \tilde{m}^2$

$$d_N \sim 2 \left( \frac{100 \text{ GeV}}{\tilde{m}} \right)^2 \sin \phi_{A,B} \times 10^{-23} \text{ ecm.}$$

exp:  $d_N < 1.1 \times 10^{-25} \text{ ecm}$

$\tilde{m} > 0 (1 \text{ TeV})$   
 $\phi_{A,B} < 0 (10^{-2})$

Buchmüller, Wyler  
 Polchinski, Wise  
 Fischer, Tavan, Thomas

# ORIGIN OF FLAVOR

SUSY

BREAKING

NO RELATION

SUSY BREAKING  
IS FLAVOR BLIND

(ex.: MSSM with FLAVOR  
UNIVERSALITY  $\tilde{m}, A$  ;  
GMSB)



- still room for NEW SOURCES OF CP  $\neq$  (at least 2 new CP  $\neq$  phases - unrelated to the flavor structure)
- SUSY FCNC contributions ( $\chi^+ \tilde{t}_R$ )

SUSY BREAKING  
KNOWS FLAVOR



SUSY breaking terms  
introduce a NEW  
FLAVOR STRUCTURE  
in addition to the  
Yukawa flavor structure  
of the SM

$$A \Rightarrow A_{ij} \neq h_{ij}$$
$$\tilde{m} \Rightarrow \tilde{m}_{ij}^2 \neq \delta_{ij} \tilde{m}^2$$



$a_\mu \equiv (g_\mu - 2)/2$  : CANDIDATE FOR  
 SUSY { (severe) CONSTRAINTS  
 MANIFESTATION

even if { SUSY BREAKING IS FLAVOR BLIND  
 NO SUSY CPs ARE PRESENT

$a_\mu^{\text{exp}}$  (Average) =  $116\,592\,023(151) \times 10^{-11}$  (Cern '77 + BNL '98, '99)

→ ultimate goal  $E821 \pm 40 \times 10^{-11}$   
 (final scheduled run with  $\mu^-$  during 2001)

→ inclusion of data from the 2000 run expected to lead to  $\pm 80 \times 10^{-11}$

$a_\mu^{\text{SM}} = a_\mu^{\text{QED}} + a_\mu^{\text{Had}} + a_\mu^{\text{EW}} = 116\,591\,597(67) \times 10^{-11}$   
 (Gzarnecki, Marciano)  $a_\mu^{\text{Had}}(\text{vac. pol.}) = 6924(62) \times 10^{-11}$  (Davier + Höcker)  
 (but  $a_\mu^{\text{Had}}(\text{vac. pol.}) = 6988(111) \times 10^{-11}$  (Jegerlehner 2000, preliminary))

$a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = 426 \pm 165 \times 10^{-11}$  (2.6σ)

$215 \times 10^{-11} \leq a_\mu(\text{New Physics}) \leq 637 \times 10^{-11}$

(Incomplete) bibliography on  $a_{\mu}$  in SUSY

Fayet '80; Grifols, Mendez '82;

Ellis, Hagelin, Nanopoulos '82;

Barbieri, Maiani '82;

Romao, Barroso, Bento, Branco '85;

Kosover, Krauss, Sakai '83;

Yuan, Arnowitt, Chamseddine, Nath '84;

Vendramin '89; Grifols, Sola, Mendez '86;

Morris '88; Frank, Kalman '88;

Lopez, Nanopoulos, Wang '94  $\rightarrow$  tan  $\beta$

Moroi '96;

Cho, Hagiwara, Hayakawa '00;

Ibrahim, Nath '00;

Carona, Giudice, Wagner '97 **GMSB**

Brignole, Perazzi, Zwirner '99

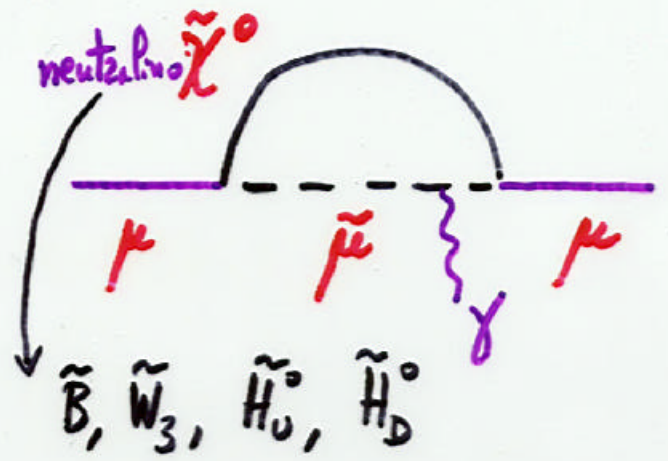
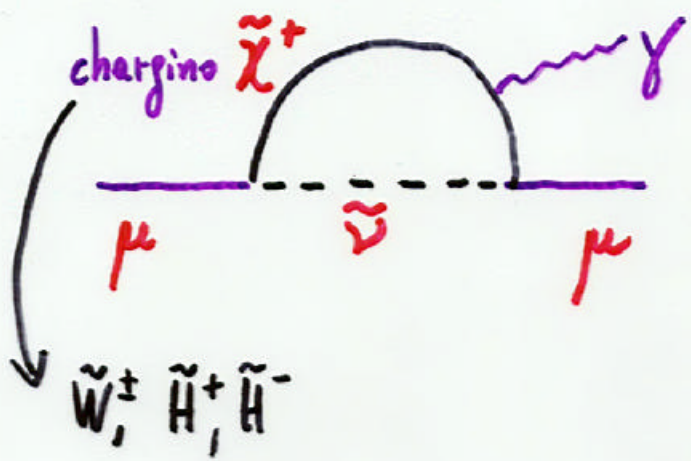
Mahantappa, Oh '00

Chattopadhyay, Nath '96

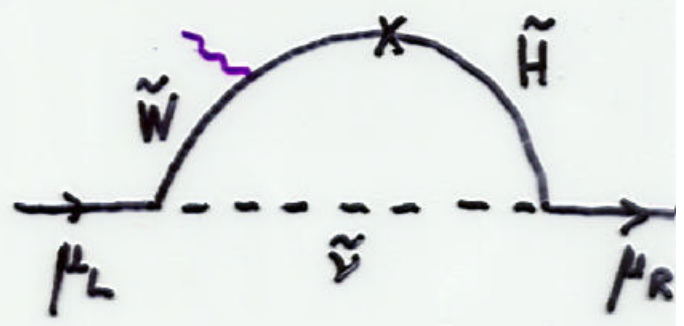
Goto, Okada, Shimizu '99; Blazek '99

Chattopadhyay, Ghosh, Roy '00

# SUSY CONTRIBUTION TO $a_\mu$



(generally) dominant contribution



for large  $\tan\beta$ :

$$|a_\mu^{\text{SUSY}}| \approx \frac{\alpha(M_Z)}{8\pi \sin^2\theta_W} \frac{m_\mu^2}{\tilde{m}^2} \tan\beta \left(1 - \frac{4x}{\pi} \ln \frac{\tilde{m}}{m_\mu}\right)$$

$\tilde{m}$  average SUSY mass in the loop  
 $\rightarrow \tilde{\chi}^+, \tilde{\nu}$  taken to be degenerate



Czarnecki, Marciano

$$|a_\mu^{\text{SUSY}}| \approx 130 \times 10^{-11} \left(\frac{100 \text{ GeV}}{\tilde{m}}\right)^2 \tan\beta$$

for sizeable SUSY contrib.

$$\tilde{m} \approx (55 \text{ GeV}) \sqrt{\tan\beta}$$

rough relation valid only if  $m_{\tilde{\chi}} = m_{\tilde{\nu}}, \dots$

FCNC and  $CP \neq$

WHEN SUSY BREAKING IS  
FLAVOR BLIND



STILL LARGE CONTRIBUTIONS  
FROM THE EXCHANGE OF SUSY PARTICLES  
ARE POSSIBLE IN SOME FCNC processes  
(most relevant case:  $b \rightarrow s + \gamma$ ), in  
particular if LIGHT STOP AND CHARGINO  
are present, or in Flavor conserving

and Flavor Changing  $CP \neq$  ( $d_n^e, d_e^e$  \*)  
 $\downarrow \downarrow$   
 $b \rightarrow s \gamma$   
ACP  
(see figs)

\*  $d_n^e, d_e^e \rightarrow \phi_A, \phi_\mu$  even in CMSSM: close to  
the exp. bound for  $m_{\tilde{q}, \tilde{g}} \leq 1 \text{ TeV}$   
 $\phi_\mu \sim 10^{-1} - 10^{-2}$

\* LIGHT STOP ( $\tilde{t}_2$ ) and CHARGINO (exp. bounds  $m_{\tilde{E}_2}, m_\chi > 1$ )

Bartl, Gajdosik, Lunghi, A.M., Porod,  
 Stockinger, Stremnitzer, Vives (in preparation)

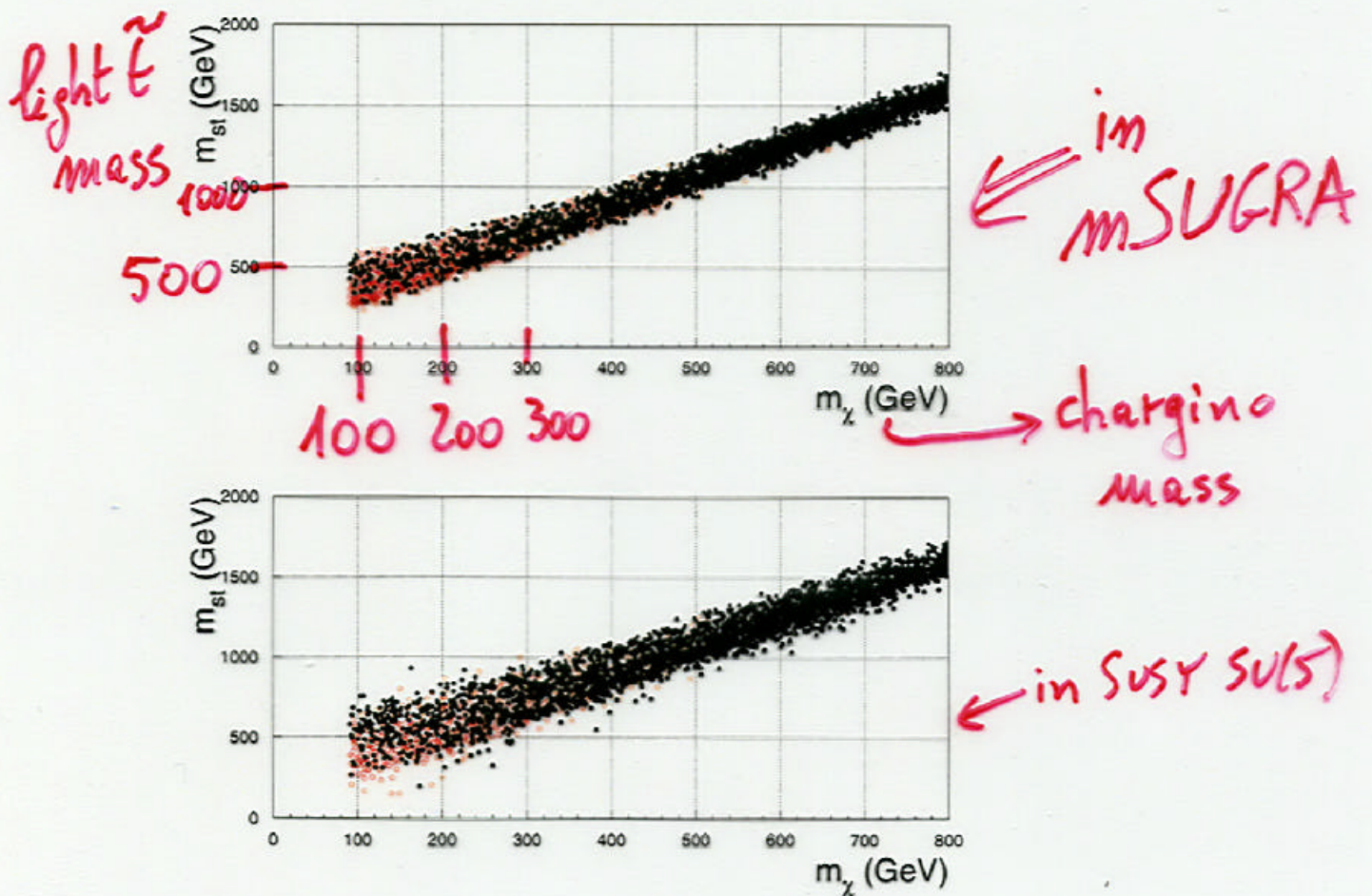


Figure 1: Chargino mass versus lightest stop mass as for the parameter space described in the text in the CMSSM and SU(5) cases.

Bartl et al

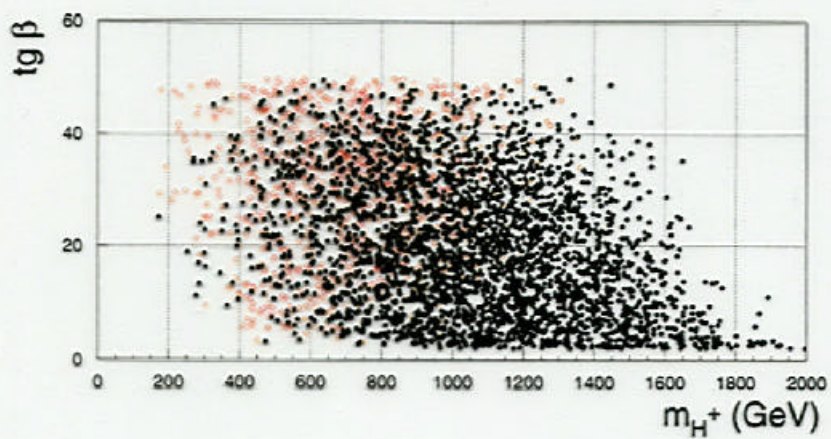
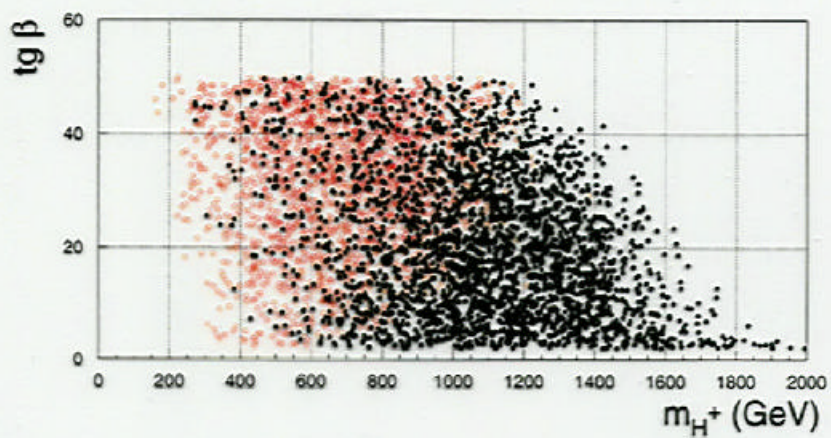


Figure 2: Charged Higgs mass as a function of  $\tan\beta$  for the parameter space described in the text in the CMSSM and SU(5) cases.

$$\Delta M_d = \Delta M_d^{SM} [1 + \Delta^{SUSY}]$$

$$\Delta M_s = \Delta M_s^{SM} [1 + \Delta^{SUSY}]$$

$$|\epsilon_K| = \frac{G_F^2 P_K^2 M_K M_W^2}{6\sqrt{2}\pi^2 \Delta M_K} \hat{B}_K (A^2 \lambda^6 \bar{q}) (y_c \{ \hat{q}_{ct} f_3(y_c, y_t) - \hat{q}_{cc} \}$$

$$+ \hat{q}_{tt} f_2(y_t) [1 + \Delta^{SUSY}] A^2 \lambda^4 (1 - \bar{p}))$$

$\Delta^{SUSY} > 0 \Rightarrow$  SUSY contributions add **CONSTRUCTIVELY** to the SM contribution in the entire allowed SUSY parameter space

$$\Delta = 0 \rightarrow 14.6 \leq \Delta M_s \leq 31.2 \text{ ps}^{-1} \quad \text{SM}$$

$$\Delta = 0.2 \rightarrow 14.6 \leq \Delta M_s \leq 35.5 \text{ ps}^{-1} \quad \left. \begin{array}{l} \text{mSUGRA} \\ \text{non-minimal SUGRA} \end{array} \right\}$$

$$\Delta = 0.4 \rightarrow 14.9 \leq \Delta M_s \leq 39.4 \text{ ps}^{-1} \quad \left. \begin{array}{l} \text{non-SUGRA} \end{array} \right\}$$

$$\Delta = 0.75 \rightarrow 15.1 \leq \Delta M_s \leq 48.6 \text{ ps}^{-1}$$

ALI-LONDON

exp:  $\Delta M_s > 14.9 \text{ ps}^{-1}$  (at 95% C.L.)  
 best minimum in the bf-likelihood function  $\Delta M_s = 17.7 \text{ ps}^{-1}$  (2.5 $\sigma$  away from 0)

SUSY theories with **MINIMAL FLAVOR VIOLATION** (no new flavor structure)

Ex:

•  $B_s - \bar{B}_s$  mixing  $\Delta m_{B_s} \approx (28 \pm 5) \frac{\Delta m_{B_d}}{[(1-\rho)^2 + \eta^2]}$

Branco, Cho, Kizukuri, Oshimo ;

Branco, Grimus, Lavoura ;

Brignole, Feruglio, Zwirner ;

Misiak, Pokorski, Rosiek; Chankowski, Pokorski can be smaller than in SM

new MSSM contributions to  $\Delta m_{B_d}$  and  $\epsilon_K$

Ali-Bondan: effects up to 60% of the SM contribution

•  $CP \neq$  in  $B \rightarrow X_s + \gamma$

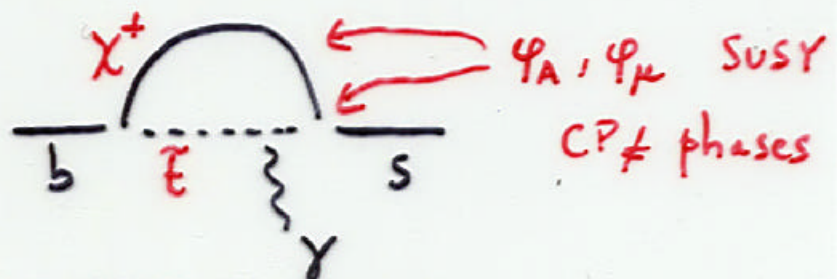
$A_{CP}^{b \rightarrow s \gamma}$  in SM is very small  $< 1\%$

(because of a combination of CKM and GIM suppressions)

Soares; Kagan, Neubert; Ali, Asatrian, Greub

in Constrained MSSM:

Kagan, Neubert



if  $\varphi_\mu = 0$  (to avoid severe problems with  $d_e^n$ )

$\Rightarrow A_{CP}^{b \rightarrow s \gamma}$  can still grow up to few (4 or 5) %

Aoki, Cho, Oshimo

if both  $\varphi_A, \varphi_\mu \neq 0 \Rightarrow A_{CP}^{b \rightarrow s \gamma}$  can reach 10 %

Chua, He, Hou

Baek, Ko



MSSM without new flavor structure  
but with new, large CP ≠ phases

( $d_n^e$  tamed by cancellations among different contributions:  
Ibrahim, Nath; Brhlik, Good, Kane; Brhlik, Everett, Kane, Lykken;  
Accomando, Arnowitt, Dutta



GENERAL MSSM with  $\delta_{CKM} = 0$   
WITH ALL POSSIBLE PHASES IN  
THE SOFT BREAKING TERMS

$$(A_u e^{i\varphi_{Au}}, A_D e^{i\varphi_{AD}}, A_E e^{i\varphi_{AE}}, \\ m_g e^{i\varphi_g}, m_{\tilde{W}} e^{i\varphi_{\tilde{W}}}, m_{\tilde{B}} e^{i\varphi_{\tilde{B}}}, \mu = |\mu| e^{i\varphi_{\mu}})$$

BUT NO NEW FLAVOR  
DEHIR, A.M., VIVES STRUCTURE in addition  
to the usual Yukawa matrices

IT IS NOT POSSIBLE TO GIVE  
SIZEABLE CONTRIBUTIONS TO  $\epsilon, \epsilon'/\epsilon,$   
HADRONIC  $B^0$  CP ASYMMETRIES

(only  $A_{CP}^{b \rightarrow sg}$ , isospin violation in  $B \rightarrow \rho\gamma$  Ali, Handberg, London

⇒ if some new flavor structure is present (even if phase, flavor ind  
⇒ probably large effects Brhlik, Everett, Kane, King, Lebedev

# IF SUSY BREAKING

IS NOT FLAVOR BLIND



HOW SEVERE  
ARE THE CONSTRAINTS  
ON THE NEW  
FLAVOR and  $CP \neq$   
SUSY STRUCTURE?



- constraint on the underlying theory (bottom-up approach)
- hints for flavor symmetries

HOW LARGE  
CAN THE SUSY  
CONTRIBUTIONS  
TO FCNC and  
 $CP \neq$  BE?



what is the  
"maximal  
hope" we  
have to observe  
deviations from  
the SM predictions  
in FCNC and  
 $CP \neq$  phenomena

WHAT CAN WE  
"REASONABLY"  
EXPECT TO  
SEE IN FCNC  
and  $CP \neq$   
as SUSY  
deviations from SM



i.e. taking  
SUSY models  
with new flavor  
structures which  
do not  
"violently"  
deviate from  
the SM flavor  
pattern