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4th International Workshop on B physics and CP violation

Ise-Shima, Japan, February 19 - 23, 2001

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**LOW ENERGY SUPERSYMMETRY AND THE  
TEVATRON BOTTOM QUARK CROSS SECTION**

Edmond L. Berger

February 23, 2001

with B. Harris, D. Kaplan, Z. Sullivan, T. Tait, and C. Wagner

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hep-ph/0012001

<http://gate.hep.anl.gov/berger/seminars/BCP4.ps>

## 1. Motivation and Constraints

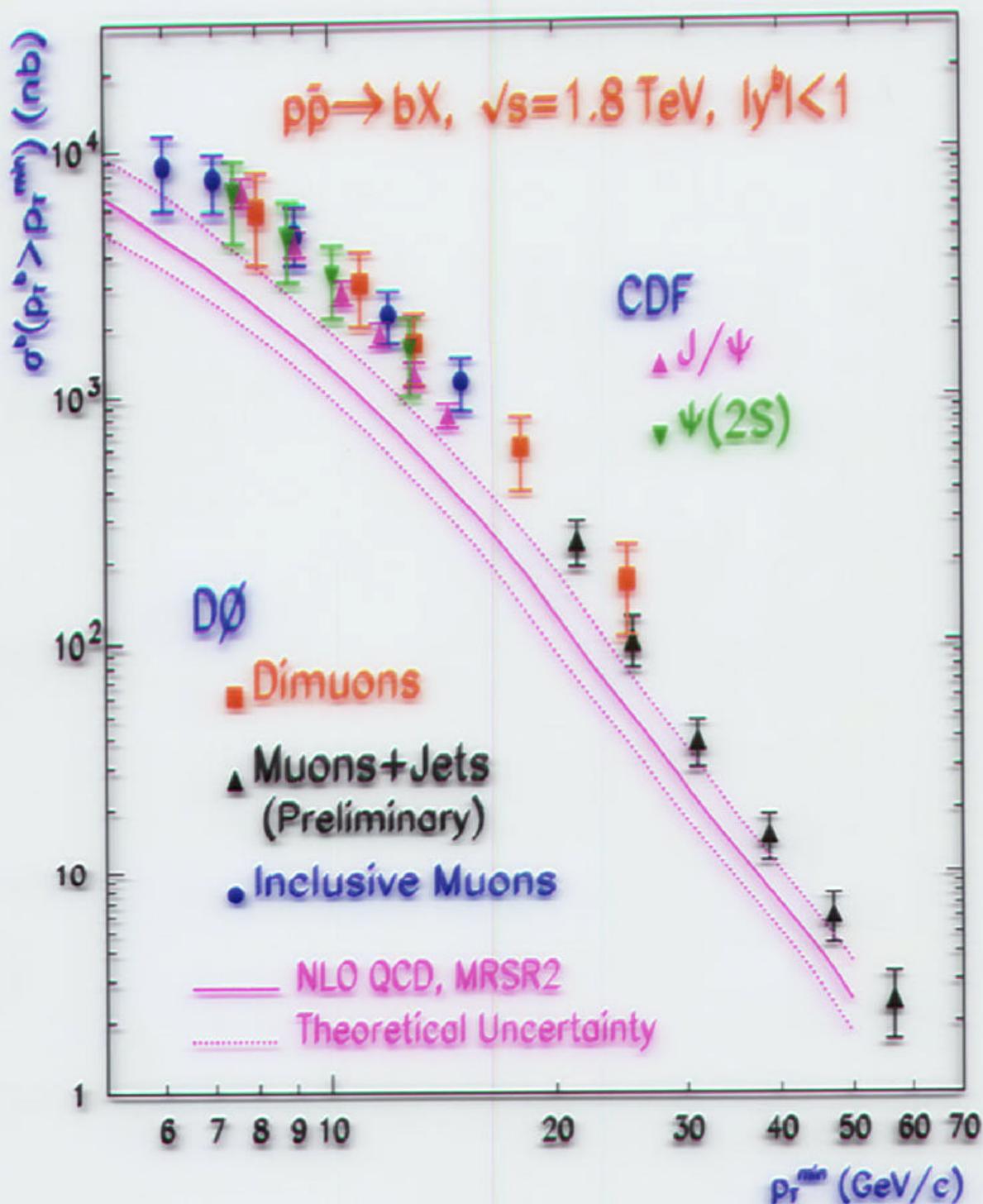
- Measured cross section for bottom quark production at hadron colliders exceeds the (central value of) predictions of next-to-leading order (NLO) QCD by about a factor of 2  
[→ Fig.]
- NLO contributions are large, and it is not excluded that further NNLO effects may do the trick, but ...
- Longstanding discrepancy has resisted satisfactory resolution within the SM → room for new physics?
- Propose a possible explanation within the context of the minimal supersymmetric standard model (MSSM):  
assume existence of a light color-octet, spin-1/2 gluino ( $\tilde{g}$ ) and a light color-triplet spin-0 bottom squark ( $\tilde{b}$ ):

$$p + \bar{p} \Rightarrow \tilde{g} + \tilde{g} + X,$$

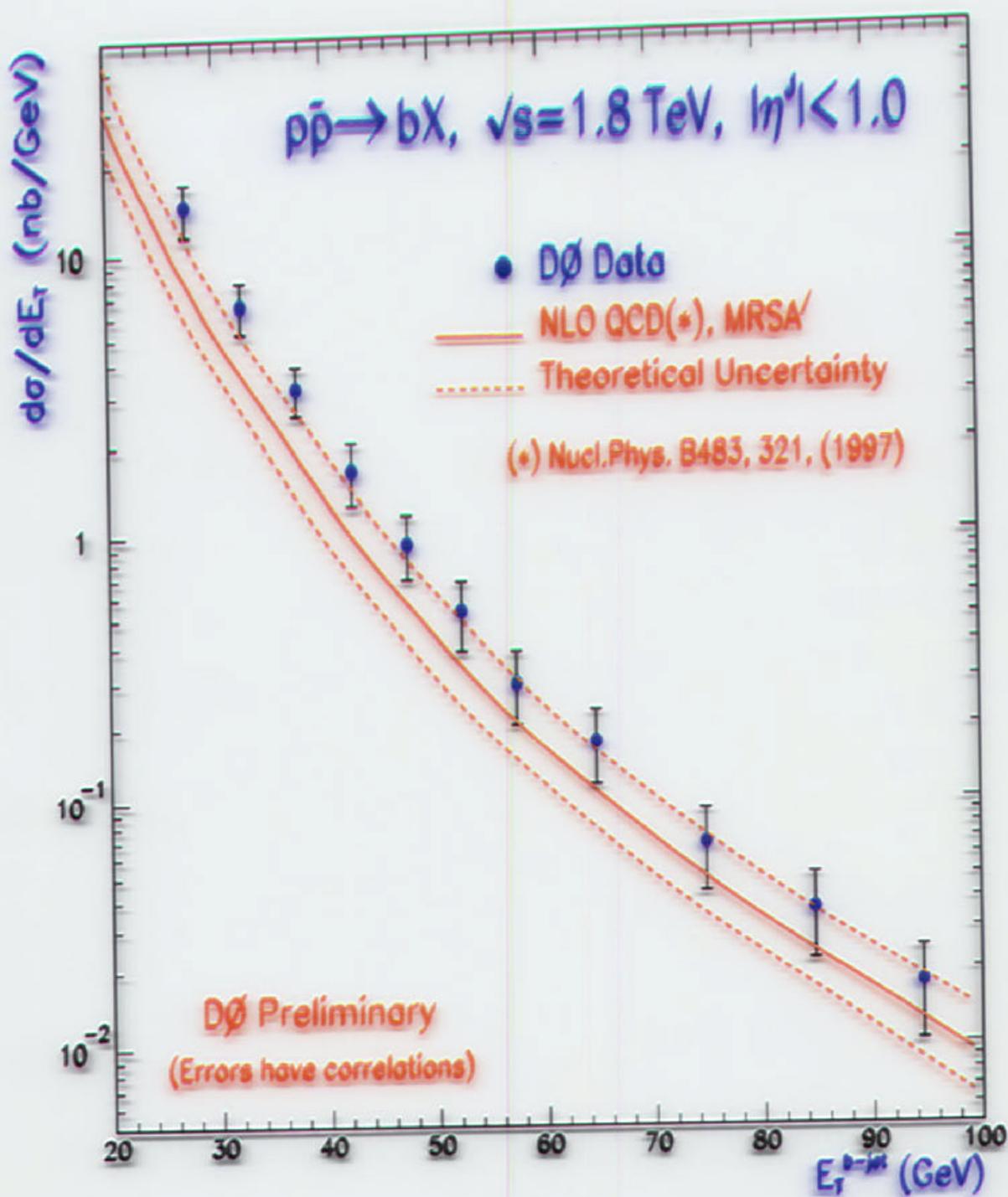
$$\tilde{g} \Rightarrow b + \tilde{b}$$

- Masses constrained by "fit" to the hadron collider data:
  - $m_{\tilde{g}} \simeq 12$  to  $16$  GeV;  $m_{\tilde{b}} \simeq 2$  to  $5.5$  GeV
- $\tilde{b}$  is long-lived on the scale of colliders or it decays hadronically (via R-parity violation?)

# INTEGRATED TRANSVERSE MOMENTUM SPECTRUM FOR $b$ QUARKS



# DIFFERENTIAL $b$ -JET TRANSVERSE MOMENTUM DISTRIBUTION



## LEP Constraints on Bottom Squark Couplings

(Carena, Heinemeyer, Wagner, and Weiglein, hep-ph/0008023)

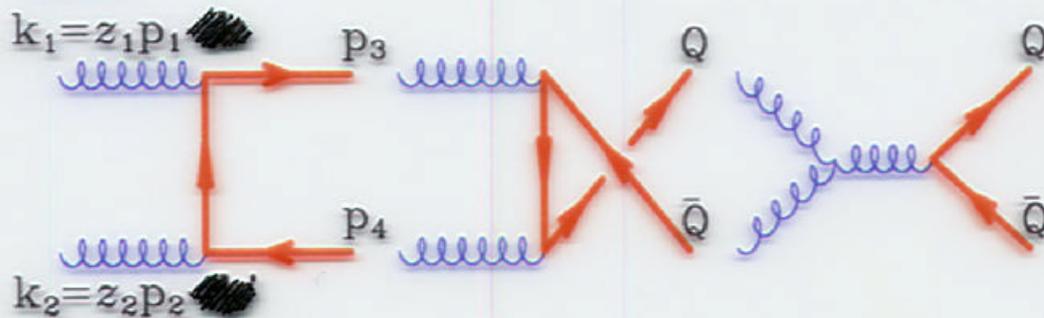
- Light  $\tilde{b}$  would be ruled out by LEP1 data unless its coupling to the  $Z$  boson is small
- Squark couplings to the  $Z$  depend on the mixing angle  $\theta_{\tilde{b}}$
- Let  $\sin\theta_{\tilde{b}} = s_{\tilde{b}}$  be the left-handed component of the lightest  $\tilde{b}$  mass eigenstate;  $s_W^2 = \sin^2\theta_W$
- Coupling  $g_{Z\tilde{b}_1\tilde{b}_1} \sim [T_3 s_{\tilde{b}}^2 - Q_{\tilde{b}} s_W^2]$   
( $T_3 = -1/2$ ;  $Q_{\tilde{b}} = -1/3$ )
- Coupling to  $Z$  vanishes for  $s_{\tilde{b}}^2 \sim 1/6$
- Thus, if the light bottom squark is an appropriate mixture of left-handed and right-handed bottom squarks, tree-level coupling to the  $Z$  can be made small
- $Z - \tilde{b}_1 - \tilde{b}_2$ ,  $Z - \tilde{b}_2 - \tilde{b}_2$  couplings survive in this limit
- Require  $m_{\tilde{b}_2} > 200$  GeV to avoid  $e^+e^- \rightarrow Z^* \rightarrow \tilde{b}_1 + \tilde{b}_2$

## Further Considerations

- For a small range of values of  $s_{\tilde{b}}$ ,  $Z$ -peak observables  $\Gamma_Z, R_c, R_\ell, R_b, A^b, A_{FB}^b$  are fit about as well as in the SM
- A light  $\tilde{b}$  with some  $\tilde{b}_L$  component will contribute to  $\Delta\rho$  ( $T$  parameter), depending on the  $\tilde{t}$  sector; constrains the top squark mass to be light ( $m_{\tilde{t}} \sim m_t$ )
- Exclusion by CLEO of a light  $\tilde{b}$  with mass 3.5 to 4.5 GeV does not apply since their analysis focuses on  $\tilde{b} \rightarrow cl\tilde{\nu}$  and  $\tilde{b} \rightarrow cl$
- ALEPH LEP analysis of 4 jet events excludes a  $\tilde{g}$  with  $m_{\tilde{g}} < 6.5$  GeV, but not gluinos in the mass range of interest to us. Light  $\tilde{b}$  is not excluded by 4 jet analysis (Z. Phys C76, 1 (1997))
- Dedes and Dreiner use the renormalization group method to argue that the existence of a light  $\tilde{b}$  goes hand-in-hand with a comparatively light  $\tilde{g}$ ,  $m_{\tilde{g}} \sim 10$  GeV (hep-ph/0009001)

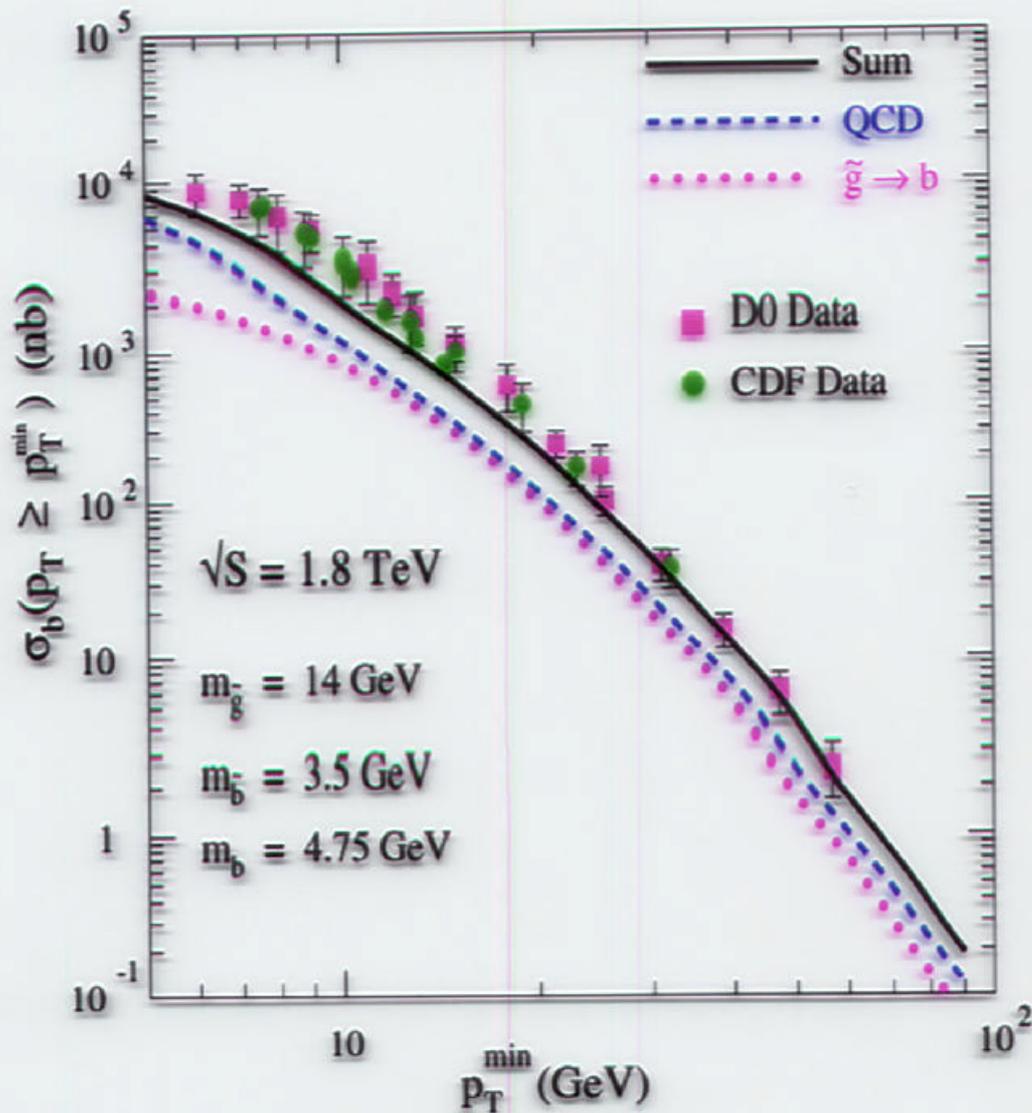
## 2. Production Processes

- Pair production of  $Q\bar{Q} = b\bar{b}, \tilde{g}\tilde{g}$  via  $gg$  scattering in LO QCD:



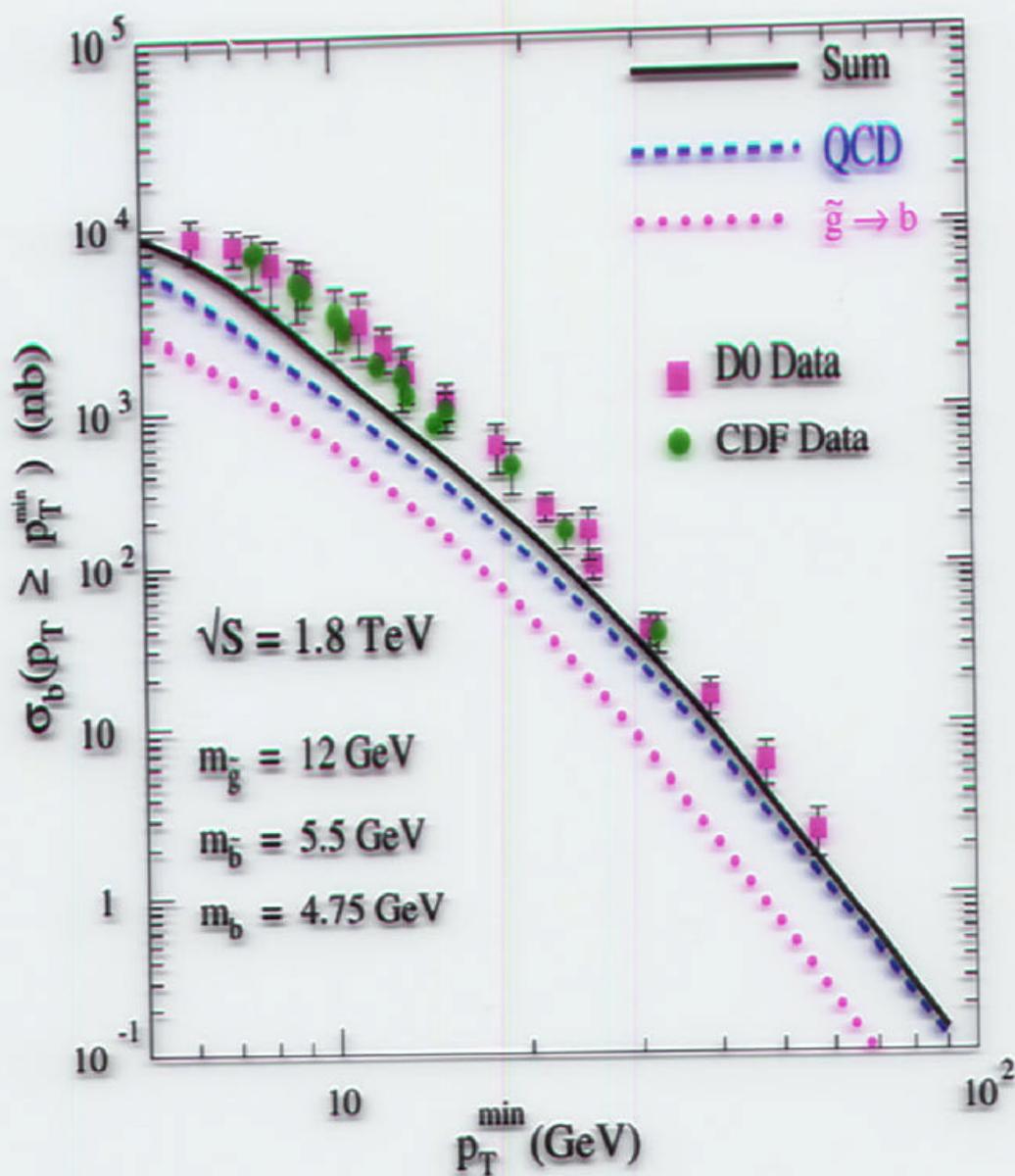
- Second set of LO diagrams for  $q\bar{q}$  initial state, but  $gg$  scattering dominates at Tevatron energies for the masses we consider. All contributions are included in our numerical calculations
- QCD NLO calculation of  $b$  cross section with CTEQ4M parton densities; renormalization/factorization scale  $\mu = \sqrt{m_b^2 + p_{Tb}^2}$ ; SUSY-QCD contributions to  $b$  production are not included – not available and expected to be small
- Fully differential NLO calculation of  $\tilde{g}$  pair production and decay  $\tilde{g} \rightarrow b + \bar{b}$  does not exist;  $\tilde{g}$  contribution computed at LO;  $\mu = \sqrt{m_{\tilde{g}}^2 + p_{T\tilde{g}}^2}$ ; and multiplied by an overall NLO enhancement ( $K$ ) factor
- $g + b \rightarrow \tilde{g} + \bar{b}$  contributes less than 2% of  $\sigma_{b\bar{b}}^{\text{qcd}}$

### 3. Differential Cross Section



- Values of  $m_{\tilde{g}} \simeq 12$  to  $16$  GeV produce  $p_{Tb}$  spectra that are enhanced near  $p_{Tb}^{\min} \simeq m_{\tilde{g}}$  where data deviate most from pure QCD; light  $\tilde{g}$  necessary to obtain a  $b$  cross section comparable to the pure QCD rate
- The rapidity distribution of the  $b$ 's and the azimuthal angular distributions  $\Delta\phi$  between the final  $b$ 's are very similar after  $p_T$  selections in the SUSY and pure QCD cases

## ANOTHER SET OF MASSES



- Choice of  $m_{\tilde{b}}$  impacts the kinematics of the  $b$ ; large values of  $m_{\tilde{b}}$  reduce the cross section and result in  $p_{Tb}$  spectra that agree less well with data; choices of  $m_{\tilde{g}}$  and  $m_{\tilde{b}}$  are coupled

#### 4. Ratio of Same-Sign to Opposite-Sign Leptons

- QCD processes produce  $b\bar{b}$  pairs
- Majorana  $\tilde{g}$  decays into  $b$  and  $\bar{b}$
- $\tilde{g}\tilde{g}$  pair production will generate  $bb$  and  $\bar{b}\bar{b}$  pairs as well as  $b\bar{b}$  pairs  $\Rightarrow$  potential increase in same-sign lepton pairs, and apparent increased rate of  $B\bar{B}$  mixing
- For highly relativistic  $\tilde{g}$ 's,  $\tilde{g}$ 's helicity is nearly the same as its chirality  $\rightarrow$  selection of  $\tilde{g}$ 's with  $p_{T\tilde{g}} \gg m_{\tilde{g}}$  reduces same sign  $b$ 's.
- Cuts chosen in Tevatron run I  $\rightarrow$  principally unpolarized  $\tilde{g}$ 's and thus, at production,  $N(bb + \bar{b}\bar{b}) \simeq N(b\bar{b})$
- Analyze effect of the new SUSY contribution in terms of  $\bar{\chi}$ 
  - $\bar{b} \rightarrow B^0, B_s, \Lambda_b, B^+$ 
    - $\rightarrow \ell^+$ , "right sign", with probability  $1 - \bar{\chi}$
    - $\rightarrow \ell^-$ , "wrong sign", with probability  $\bar{\chi}$
  - Define  $LS$ , same-sign lepton fraction
  - Conventional  $b\bar{b}$  pair production
    - $\rightarrow LS_c = 2\bar{\chi}(1 - \bar{\chi})$

• New expression

- Definition:

$$G = \frac{\sigma_{\tilde{g}\tilde{g}}}{\sigma_{\text{qcd}}}$$

- Ratio  $G$  is determined in the (cut) region of phase space where  $LS$  is measured; CDF:  $p_T > 6.5$  GeV and  $y_b \leq 1$ , both  $b$ 's

- Hadron collider experiments measure

$$\bar{\chi}_{\text{eff}} = \frac{\bar{\chi}}{\sqrt{1+G}} + \frac{1}{2} \left[ 1 - \frac{1}{\sqrt{1+G}} \right]$$

- For  $m_{\tilde{g}} = 14, 16$  GeV, we compute  $G = 0.37, 0.28$

- Adopt average value from PDG:  $\bar{\chi} = 0.118 \pm 0.005$

- **Predict:**  $\bar{\chi}_{\text{eff}}^{\text{th}} = 0.17, m_{\tilde{g}} = 14\text{GeV}$

$$\bar{\chi}_{\text{eff}}^{\text{th}} = 0.16, m_{\tilde{g}} = 16\text{GeV}$$

- Large QCD theoretical uncertainties (scale dependence, no fully NLO calculation of  $\tilde{g}$  pair production and decay):

$$\delta\bar{\chi}_{\text{eff}} \simeq \pm 0.02$$

- CDF measurement is higher than the world average (PRD 55, 2546 (1997)):

## 5. Other Implications and Remarks

### 5 a) Hadron Reactions

- Most clearcut expectation is pair production of **like-sign**  $B$ 's:  $B^+ B^+$  and  $B^- B^-$
- Very precise measurement of  $\bar{\chi}$  at run II is desirable; fraction of  $b$ 's from gluinos also changes with  $p_{Tb}$  so there should be a change of  $\bar{\chi}$  with the cut on  $p_{Tb}$
- The  $b$  jet from  $\tilde{g}$  decay into  $b\bar{b}$  will contain the  $\tilde{b} \rightarrow$  unusual material in some fraction of the  $b\bar{b}$  data sample from the  $\tilde{b}$  in the  $b$  jet
- Existence of light  $\tilde{b}$ 's means they will be pair-produced directly  $\rightarrow$  slight increase ( $< 1\%$ ) in the hadronic dijet rate
- Increased rate of  $b$  production at HERA ( $\gamma^* g \rightarrow b\bar{b}$ ) and in  $\gamma\gamma \rightarrow b\bar{b}$  at LEP, but perhaps too small if current data are confirmed; NLO calculation and better parton densities of photons are needed.

## 5 b) $\tilde{b}$ lifetime and observability

- Simple scaling from  $\mu$  or  $\tau$  lepton decay,  $\tau^{-1} \sim m^5$ , suggests  $\tau_{\tilde{b}} \sim 10^{-14}$  s ( $c\tau \sim 3\mu\text{m}$ ) for  $m_{\tilde{b}} = 3.5$  GeV
- But, R-parity conservation does not permit  $\tilde{b}$  decay unless there is an even lighter LSP
- Limits on baryon-number-violating R-parity-violating couplings  $\lambda''$  are relatively weak for 3rd generation  $\tilde{q}$ 's:  $\lambda'' < 0.5$  to  $1$  (Allanach Dedes Dreiner, PR D60, 075014 (1999))

- MSSM superpotential with baryon-number-violating R-parity-violation term

$$W_{R_p} = \lambda''_{ijk} U_i^c D_j^c D_k^c$$

- $U_i^c$  and  $D_i^c$  are right-handed-quark singlet chiral superfields;  $i, j, k$  are generation indices
- Possible  $R_p$  decay channels are  $123 : \tilde{b} \rightarrow u + s$ ,  $213 : \tilde{b} \rightarrow c + d$ , and  $223 : \tilde{b} \rightarrow c + s$

$$\Gamma(\tilde{b} \rightarrow jj) = \frac{m_{\tilde{b}}}{2\pi} \sin^2 \theta_{\tilde{b}} \sum_{j < k} |\lambda''_{ij3}|^2$$

- If  $m_{\tilde{b}} = 3.5$  GeV,  $\Gamma(\tilde{b} \rightarrow ij) \approx 0.08 |\lambda''_{ij3}|^2$  GeV
- Unless  $\lambda''_{ij3}$  is extremely small, the  $\tilde{b}$  will decay quickly and leave soft jets in the cone around the  $b$ ; jets with an extra  $c$  are possibly disfavored by CDF; detailed simulation is needed

## 5 b) $\tilde{b}$ lifetime and observability, continued

- Suppose the  $\tilde{b}$  is relatively "stable", what could happen?

- $\tilde{b}$  picks up a light  $\bar{u}$  and becomes a  $\tilde{B}^-$  "mesino" with  $J = 1/2$ , the superpartner of the  $B$  meson, a hadron with mass  $\sim 3$  to  $7$  GeV
- The mesino is **not** a muon but could fake a heavy muon as it exits the muon chambers;  $\rightarrow$  extra "muons" in a fraction of the  $b\bar{b}$  event sample, with tracks that left some trace in the hadron calorimeter?
- The mesino has baryon number 0 but acts like a heavy  $\bar{p}$  - perhaps detectable with a TOF detector in run II
- Detailed analyses should be done at hadron colliders to verify what ranges of  $\tilde{b}$  masses and lifetimes may be allowed/disfavored, similar to that done for  $\tilde{g}$ 's (c.f. Baer, Cheung, Gunion, PRD 59, 075002 (1999))
- $\tilde{b}$ -onia
- $\tilde{b}$ 's will be made in cosmic ray collisions or in particle detectors  $\rightarrow$  weird isotopes?

### 5 c) $\alpha_S$

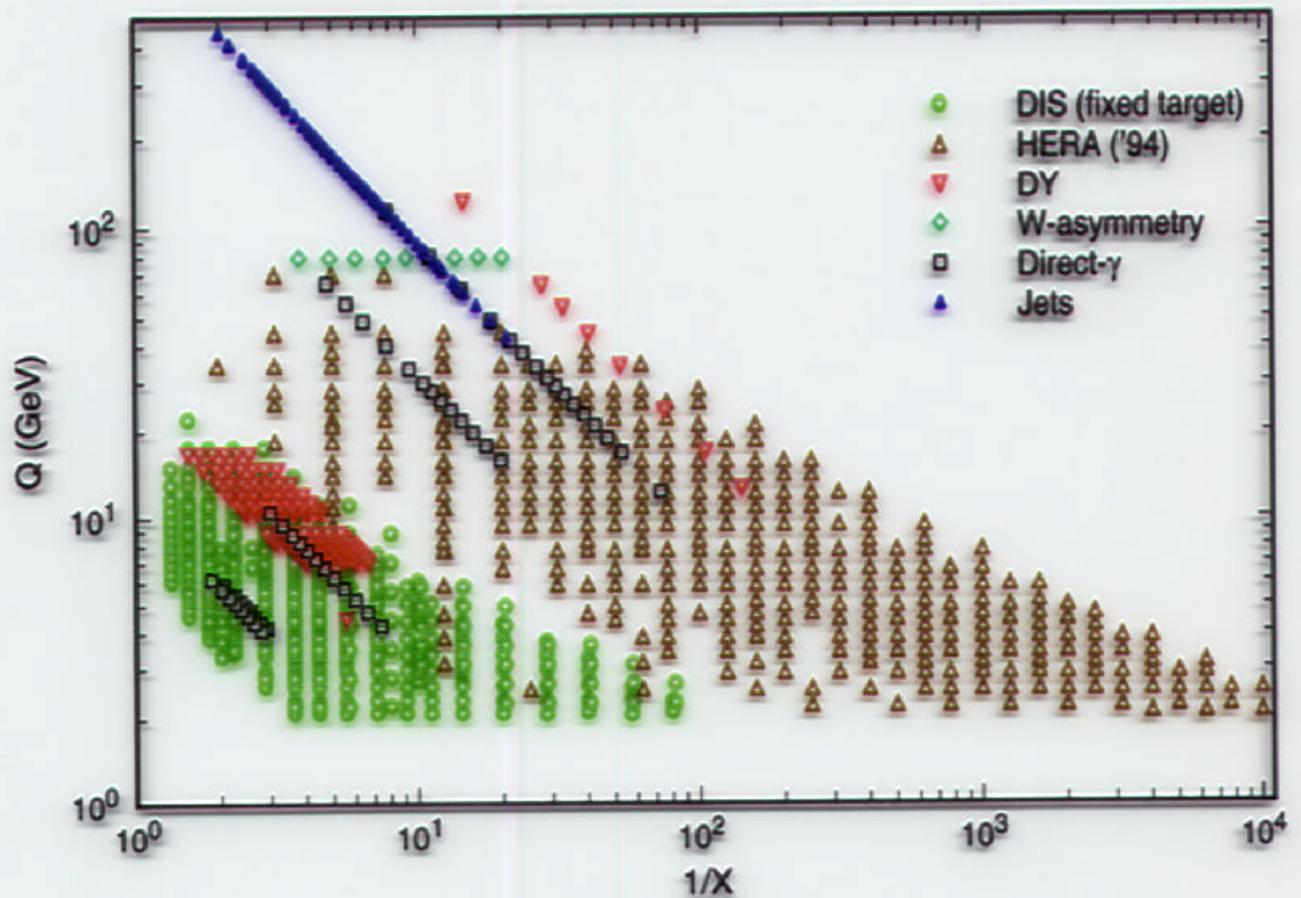
- Global fit to all observables in the SM provides  $\alpha_S(M_Z) \sim 0.119 \pm 0.006$  under SM running
- Light gluino and light bottom squark modify  $\alpha_S(M_Z)$  determined by extrapolation from experiments at energies below  $m_{\tilde{g}}$
- $\beta$  function of (SUSY) QCD:

$$\beta = \frac{g^3}{16\pi^2} \left[ -11 + \frac{2}{3}n_f + \frac{1}{6}n_s + 2 \right]$$

- The QCD running of  $\alpha_s(Q)$  is slowed
  - $\tilde{b}$  (color-triplet scalar) contributes little to the running
  - $\tilde{g}$  (color octet fermion) much more significant
- Shift of 0.007 to  $\alpha_S(M_Z) \simeq 0.125$ , within the range of uncertainty but towards the upper end
- **Separate issue** concerning  $\alpha_S$  is gauge-coupling unification: for gluinos of mass in the hundred GeV range,  $\alpha_S(M_Z)$  predicted from unification is  $> 0.13$ , but 15 GeV gluinos reduce the value to  $\leq 0.127$ , in better agreement

## INFLUENCE ON PARTON DENSITIES

- Kinematic range in the  $(x, Q^2)$  plane of data included in a typical global analysis of parton densities



- Slower running of  $\alpha_s(Q)$  means a slower evolution of parton densities at small  $x$ , an effect that might be seen in HERA data for  $Q > m_{\tilde{g}}$ . Under investigation
- Presence of scalar  $\tilde{b}$  in the proton breaks the Callan-Gross relation and yields a non-zero leading-twist longitudinal structure function  $F_L(x, Q)$

## 5 d) $R$ and Angular Distributions in $e^+e^- \rightarrow$ jets

- Deviations of  $R$  from SM expectations at large  $\sqrt{s}$ ?

$$R = \frac{e^+e^- \rightarrow \text{hadrons}}{e^+e^- \rightarrow \mu^+\mu^-}$$

- Scalars are produced in a  $p$ -wave coupled to the intermediate photon
  - Thresholds turn on slowly
  - Cross sections are small ( $\sim 1/4$  a fermion of the same charge)
- Compared to "everything else"  $\tilde{b}$  contributes

$$\left(\frac{1}{3}\right)^2 \frac{1}{4} \quad vs \quad 2 \left(\frac{2}{3}\right)^2 + 3 \left(\frac{1}{3}\right)^2$$
$$\frac{1}{36} \quad vs \quad \frac{11}{9}$$

- Data must be accurate to a few % to discriminate
- Angular distributions are potentially more powerful,  $\sin^2\theta$  vs.  $(1 + \cos^2\theta)$ ; data not inconsistent with a single pair of charge- $1/3$  squarks along with 5 flavors of  $q\bar{q}$  pairs;  $(1 + \alpha\cos^2\theta)$ , with  $\alpha \simeq 0.92$

## 5 e) $\tilde{b}$ -onia

- Could be seen as mesonic resonances in  $\gamma\gamma$  reactions (i.e.,  $e^+e^- \rightarrow e^+e^- X$ ) and in  $p\bar{p}$  formation, with masses in the 4 to 10 GeV range and  $J^P \equiv 0^+, 1^-, 2^+, \dots$
- Could show up as narrow states in  $\mu^+\mu^-$  invariant mass spectra at hadron colliders, between the  $J/\psi$  and  $\Upsilon$
- At an  $e^+e^-$  collider, the intermediate photon requires production of a  $J^{PC} \equiv 1^{--}$  state.
  - Bound states of low mass squarks with  $Q_{\tilde{q}} \equiv 2/3$  studied by Nappi with a potential model (Phys. Rev. D25, 84 (1982))
    - \*  $\Gamma_\ell \sim 24$  eV
    - \*  $\Gamma_h \sim 18$  keV
    - \*  $\Gamma_{1S+\gamma} \sim 65$  keV
  - The  $1S$  state decays hadronically
  - Because the leptonic decay widths are too small there are no bounds for  $m_{\tilde{q}} > 3$  GeV,  $Q_{\tilde{q}} \equiv 2/3$
  - For bottom squarks, the situation is stronger ( $Q_{\tilde{q}} \equiv -1/3$ ).

## 5 f) Alternative Scenarios

- Suppose only the  $\tilde{b}$  is light
  - Assume  $\tilde{b}$  decay products (e.g.,  $\tau c$  via R-parity violation) are similar to those in  $b$  decay
  - $\sigma_{\tilde{b}\tilde{b}} \simeq \sigma_{b\bar{b}}$  for  $m_{\tilde{b}} \simeq 3 \text{ GeV}$
  - Fails: excess in  $J/\Psi$  channel not produced, and  $p_{Tb}$  spectrum not reproduced
- Light  $\tilde{b}$  and light  $\tilde{g}$ , with  $m_{\tilde{b}} + m_b > m_{\tilde{g}}$  but  $m_b < m_{\tilde{b}} < m_{\tilde{g}}$ 
  - $\tilde{g} \rightarrow \tilde{b}s$  or  $\tilde{g} \rightarrow \tilde{b}d$ ;  $\tilde{b} \rightarrow b\tilde{\chi}^0$  (light  $\tilde{\chi}^0$ )
  - Requires FV coupling  $\tilde{g} - \tilde{b} - s$  to suppress  $\tilde{g} \rightarrow g\tilde{\chi}^0$
  - Killer:  $\sigma(b + \tilde{b} + \cancel{E}_T)$  much too large; excluded at run I

## 6. Summary

- There is room in the measured bottom quark production rate at hadron colliders for new physics
- We postulate the existence of light gluinos and light bottom squarks with 100% branching fraction  $\tilde{g} \rightarrow b\bar{b}$ 
  - $m_{\tilde{g}} \simeq 12$  to  $16$  GeV;  $m_{\tilde{b}} \simeq 2$  to  $5.5$  GeV
- Our SUSY scenario with  $\sigma_{\tilde{g}\tilde{g}}/\sigma_{\text{qcd}} \sim 1/3$  helps to explain the magnitude and shape of the  $b$   $p_T$  distribution at the Tevatron
- $b\bar{b}$  and  $\tilde{b}\tilde{b}$  pair production predicted
  - Visible as a mismatch of  $B^0$  oscillation parameters at the Tevatron and at  $b$  factories
  - Tevatron run I  $\tilde{\chi}$  data help constrain gluino mass
  - Should see  $B^+ B^+$  events at run II
- Search for  $\tilde{b}$ -onia
- $b$  cross sections at HERA and LEP ( $\gamma\gamma \rightarrow b\bar{b}$ ) bear watching
- Interesting SUSY consequence: light  $\tilde{t}$
- $h^0 \rightarrow \tilde{b}\tilde{b}^*$  dominates : could modify Higgs bounds